

Radiated Energy of Recent Great Earthquakes

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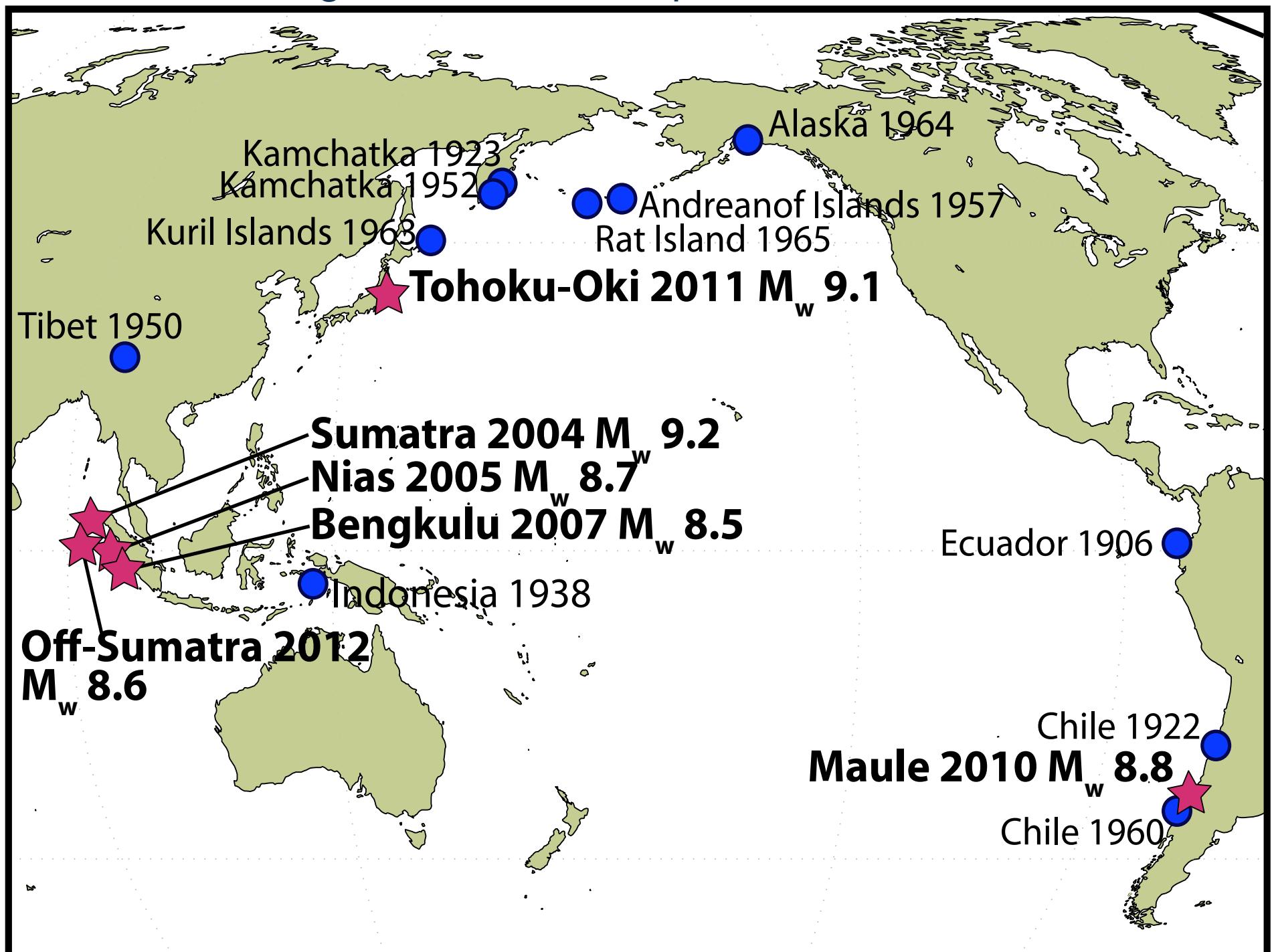


Gregory Beroza



STANFORD
SCHOOL OF EARTH SCIENCES

16 great M>8.5 earthquakes since 1900



eGf-coda Methodology for Moderate Earthquakes

(1) Create coda spectra

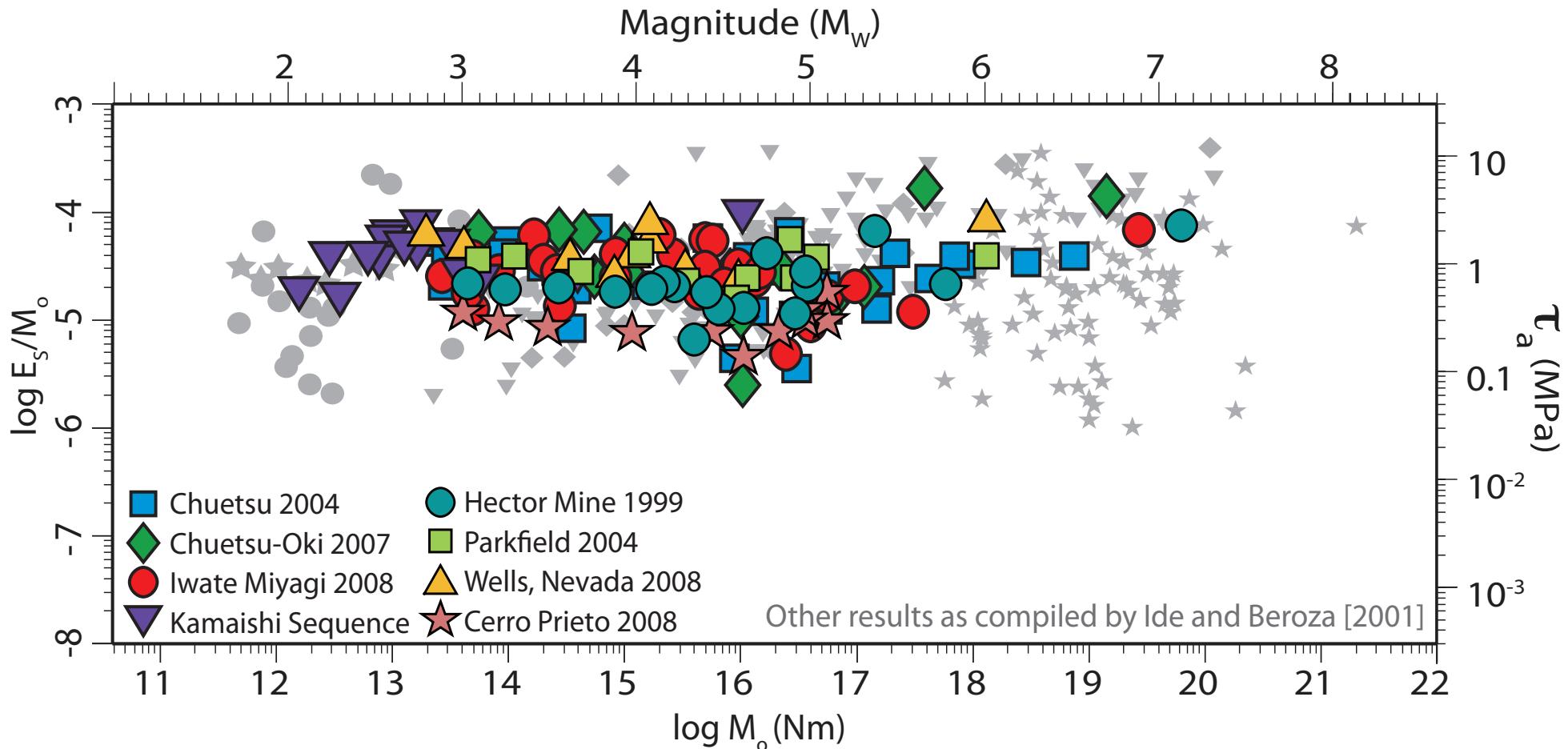
- Narrow band-pass displacement records
- Time window in each record becomes coda spectral point

(2) Empirical Green's function to remove path effects

- Small event is modeled as ideal Brune-like event
- Path effects sequentially deconvolved from larger events
- Use moment from largest event to set relative moments

(3) Source spectra → moment, corner frequency, energy

Radiated Energy and Apparent Stress



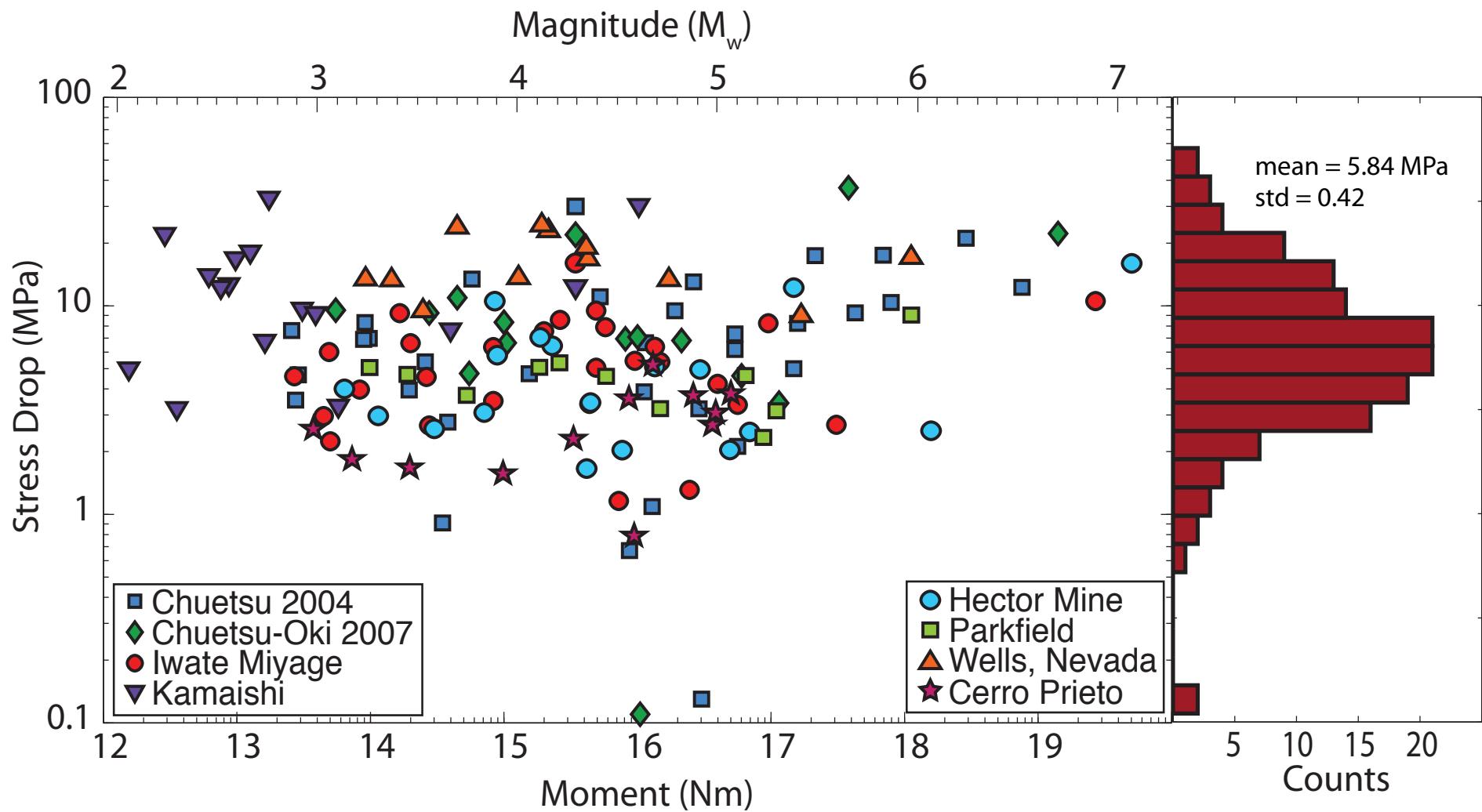
$$E_R \sim \int_0^{\infty} |\omega \cdot \dot{M}(\omega)|^2 d\omega$$

$$\tau_a = \mu \frac{E_R}{M_o}$$

Baltay et al, 2010

Baltay et al, 2011

Stress Drop

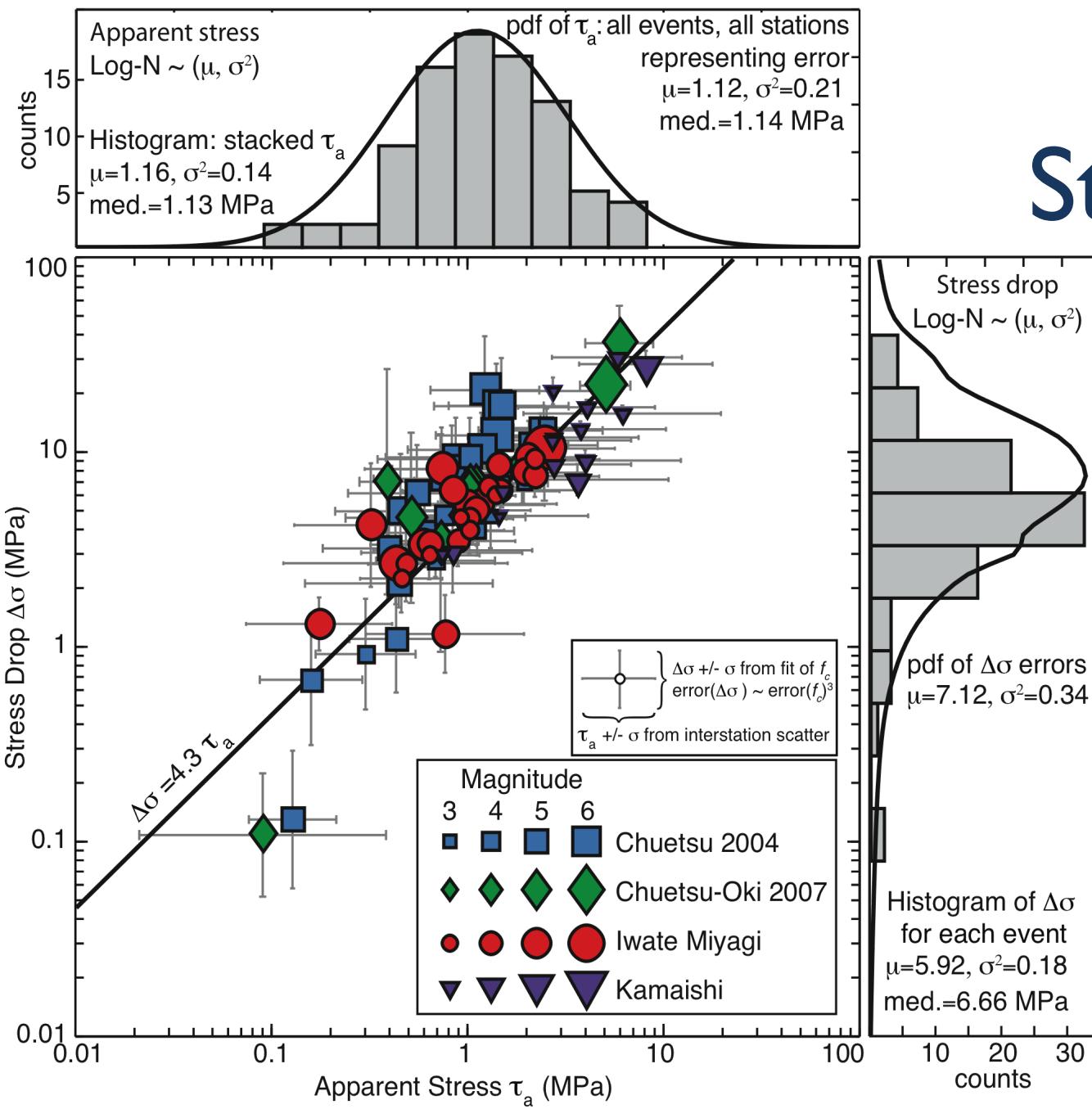


$$\Delta\sigma_{Brune} = 8.47 M_o \left(\frac{f_c}{\beta} \right)^3$$

Baltay et al, 2010

Baltay et al, 2011

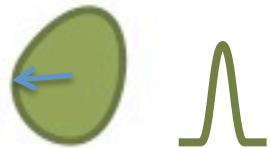
Apparent Stress and Stress Drop



- $\Delta\sigma$ and τ_a both log-normally distributed
- Follow the expected theoretical relationship

Teleseismic empirical Green's functions

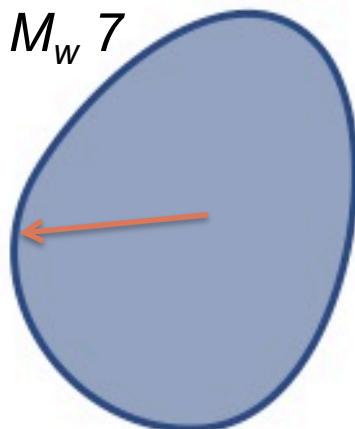
M_w 3



$r = \sim 100$ m

R upto ~ 200 km
 $r \ll R$

M_w 7

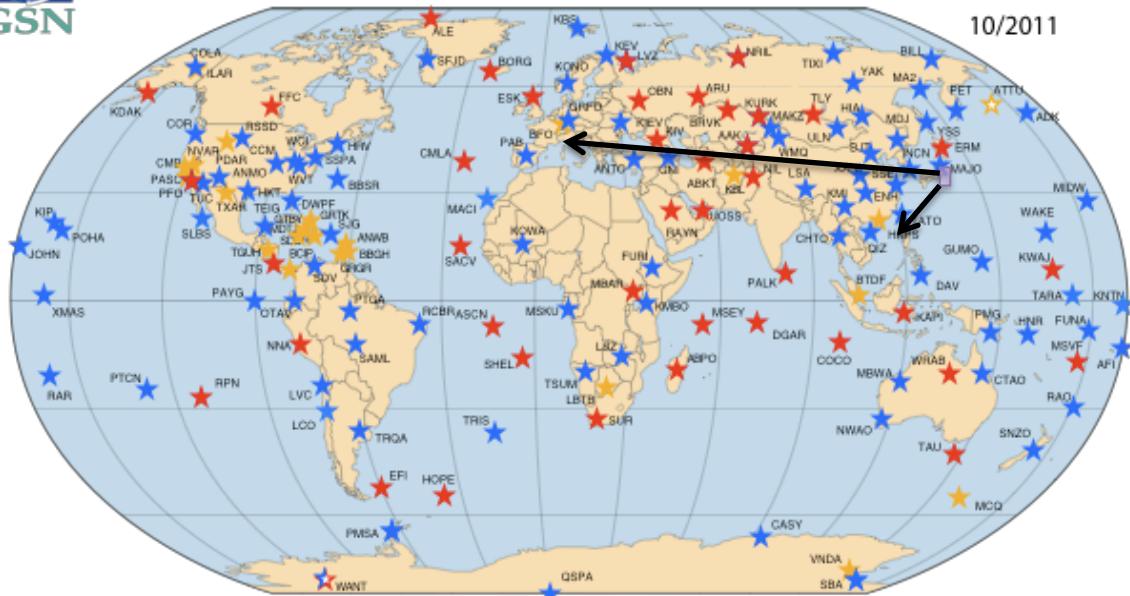


$r = \sim 10$ km

$R \sim 3000$ km to $\sim 10,000$ km
 $r \ll R$



GLOBAL SEISMOGRAPHIC NETWORK

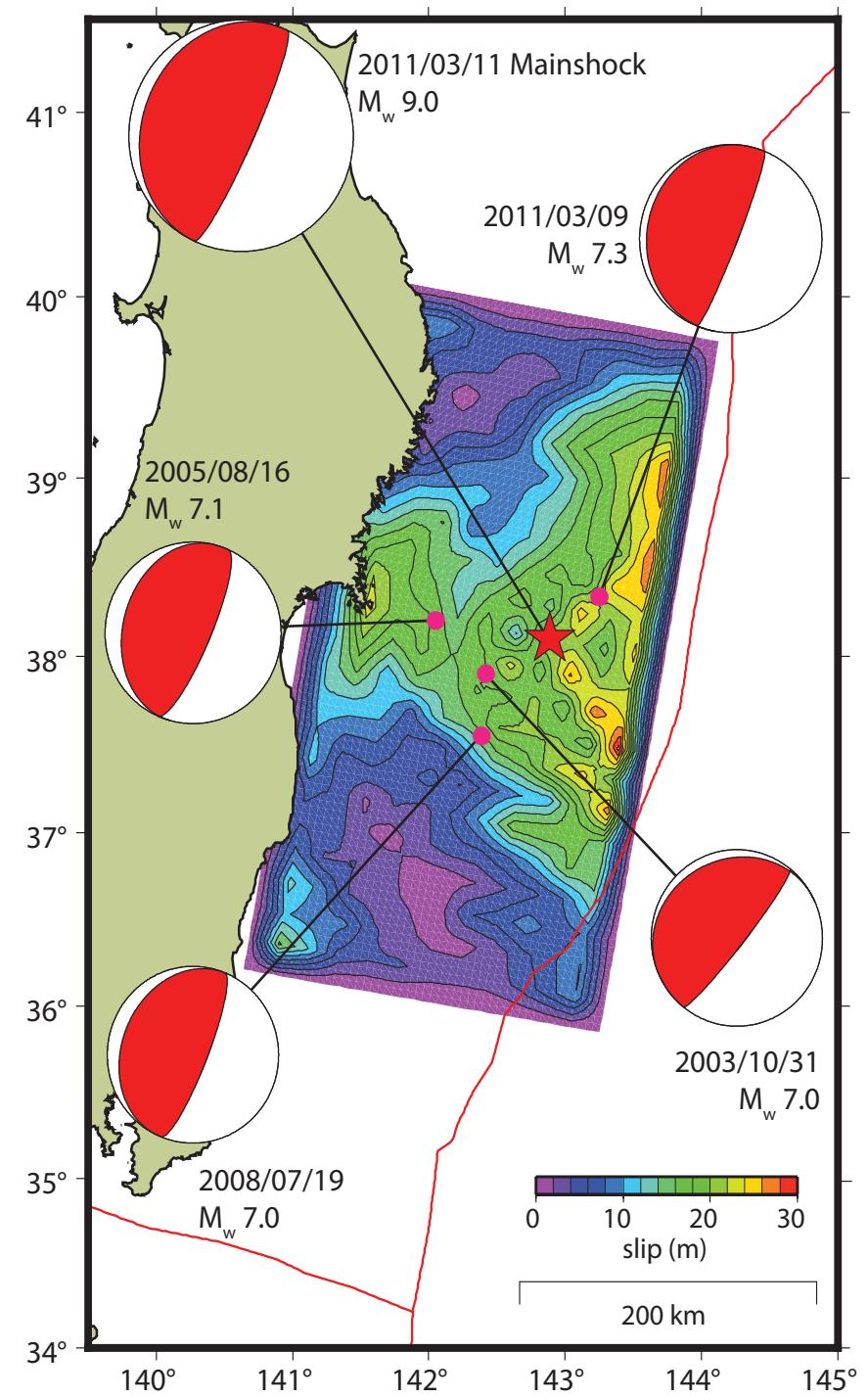
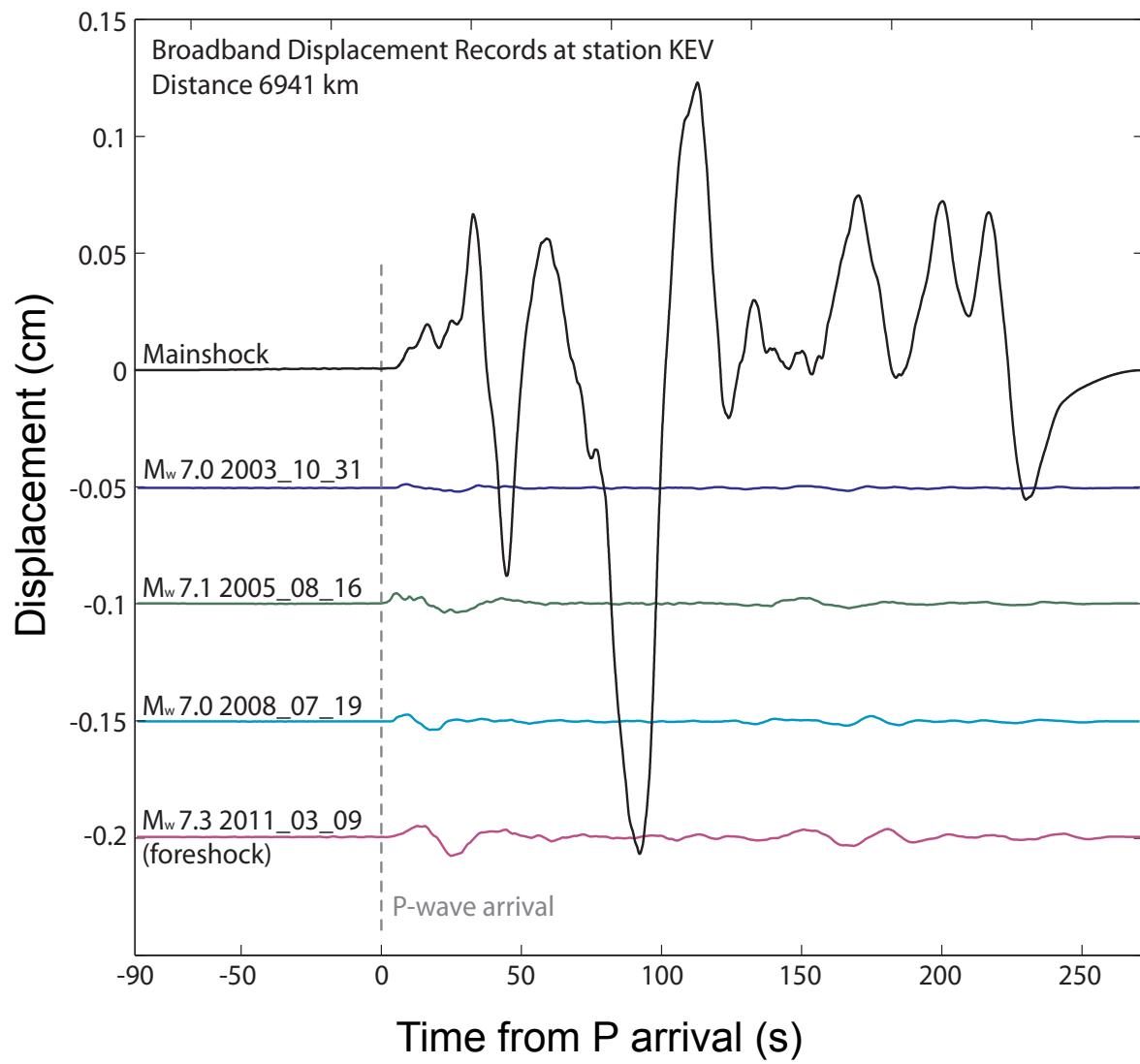


Can't use local eGf method to analyze
large $M > 7.5$ earthquakes

Assume a $\sim M 6.5 - 7.5$ can be modeled
as ideally Brune \rightarrow teleseismic eGf method

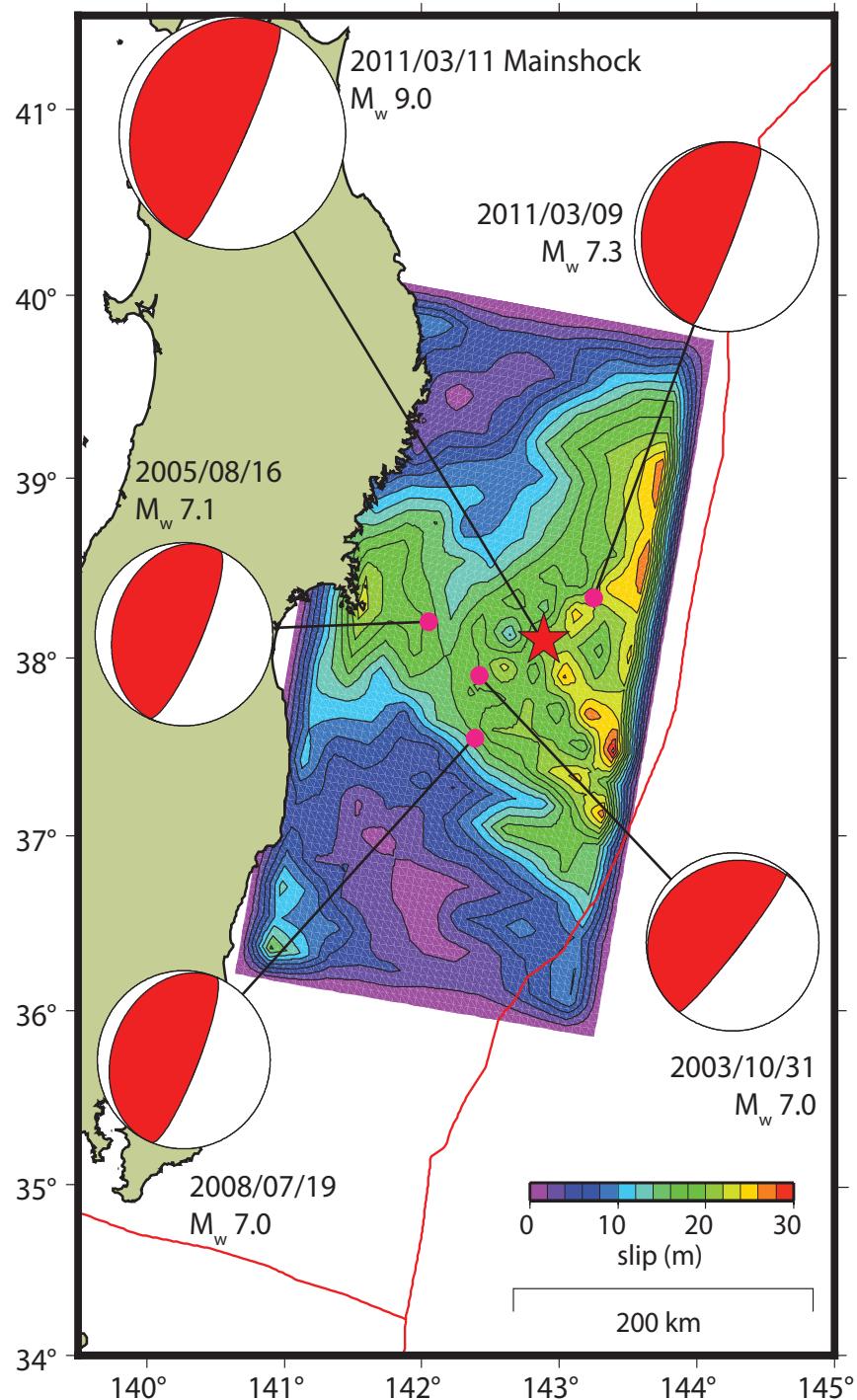
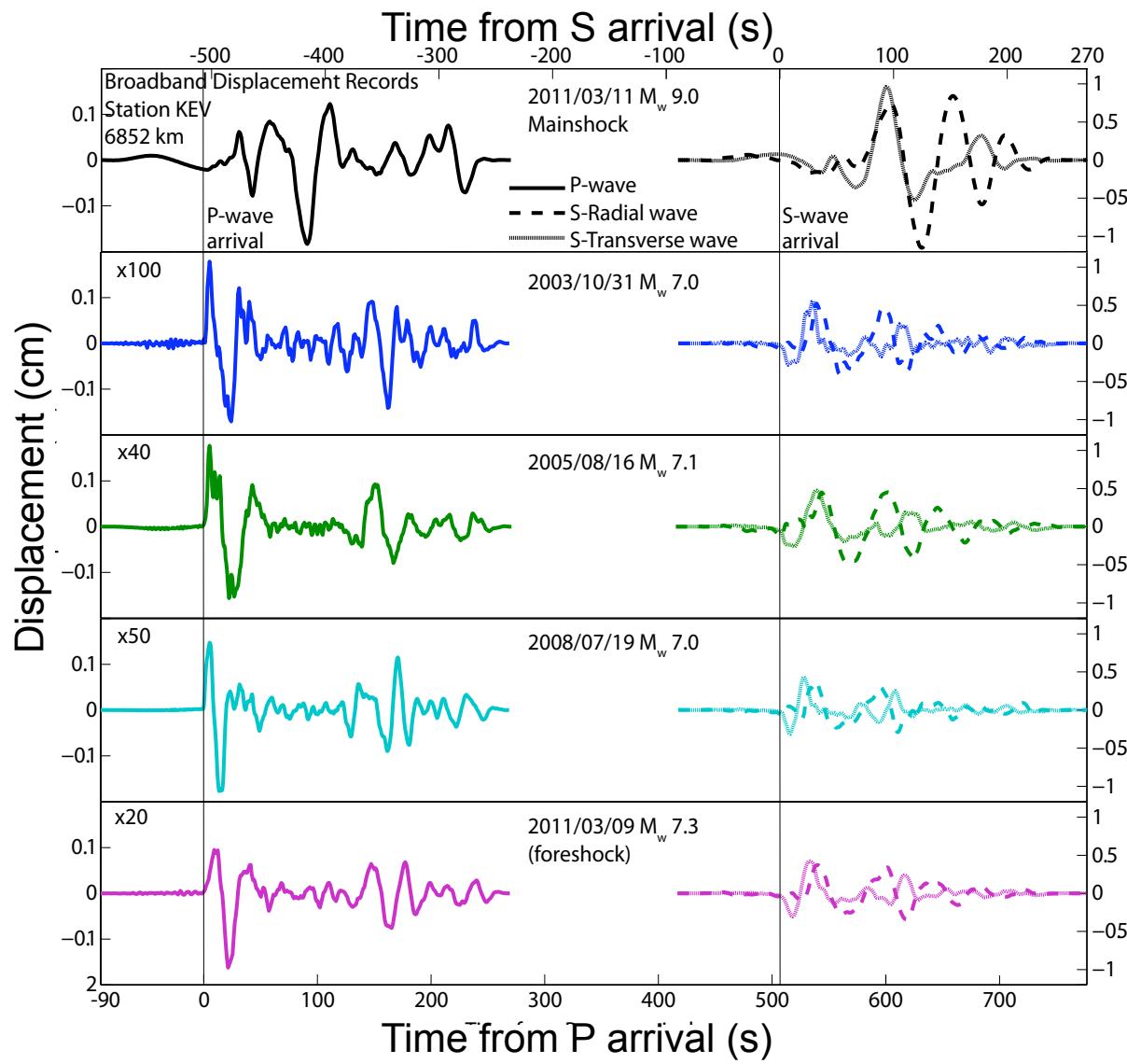
Tohoku-Oki 2011

M_w 9.1

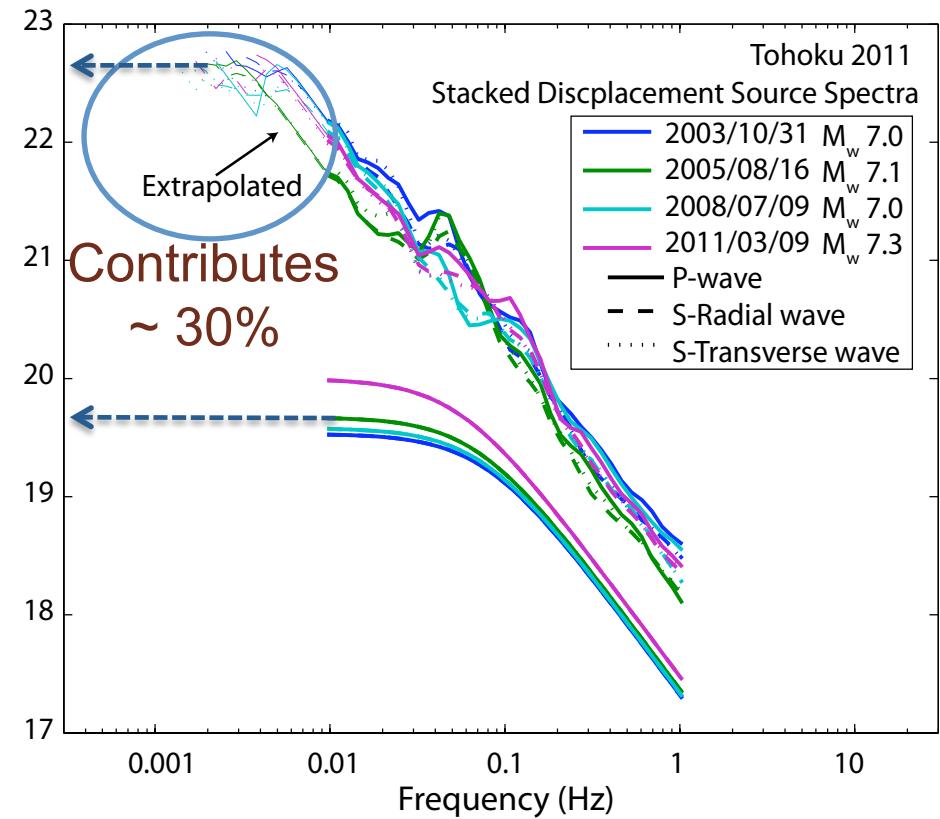
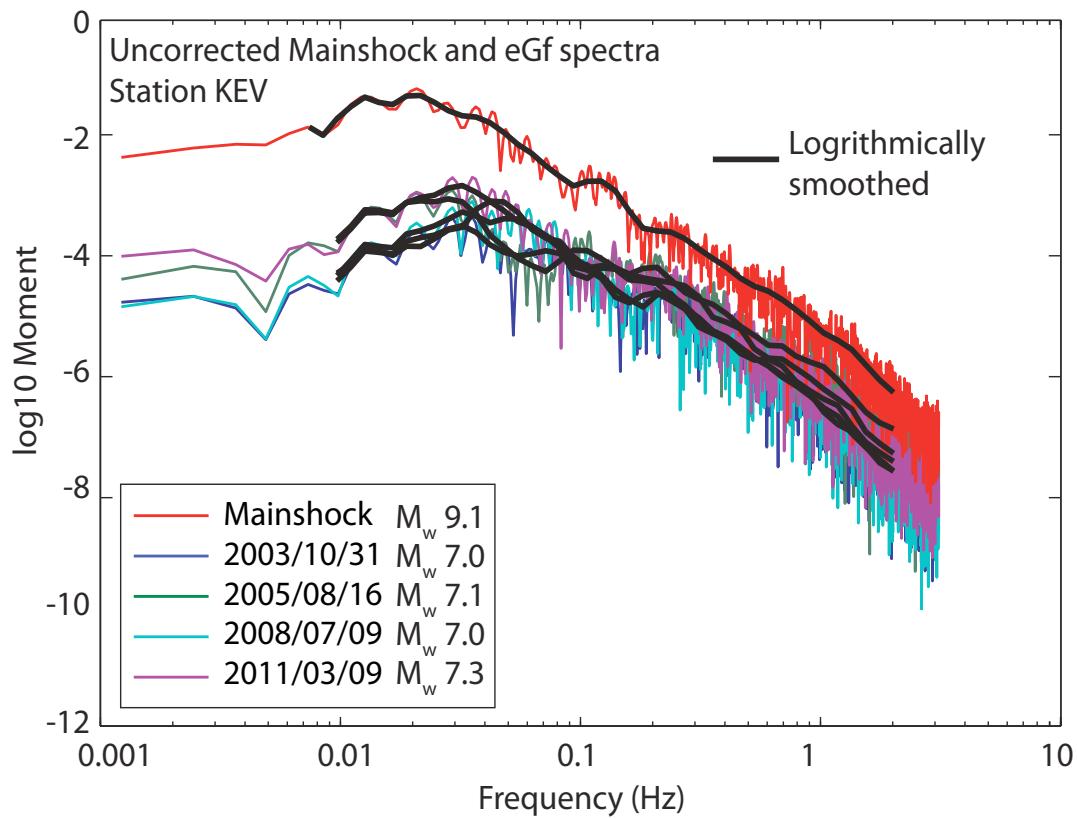


Tohoku-Oki 2011

M_w 9.1



eGf Deconvolution

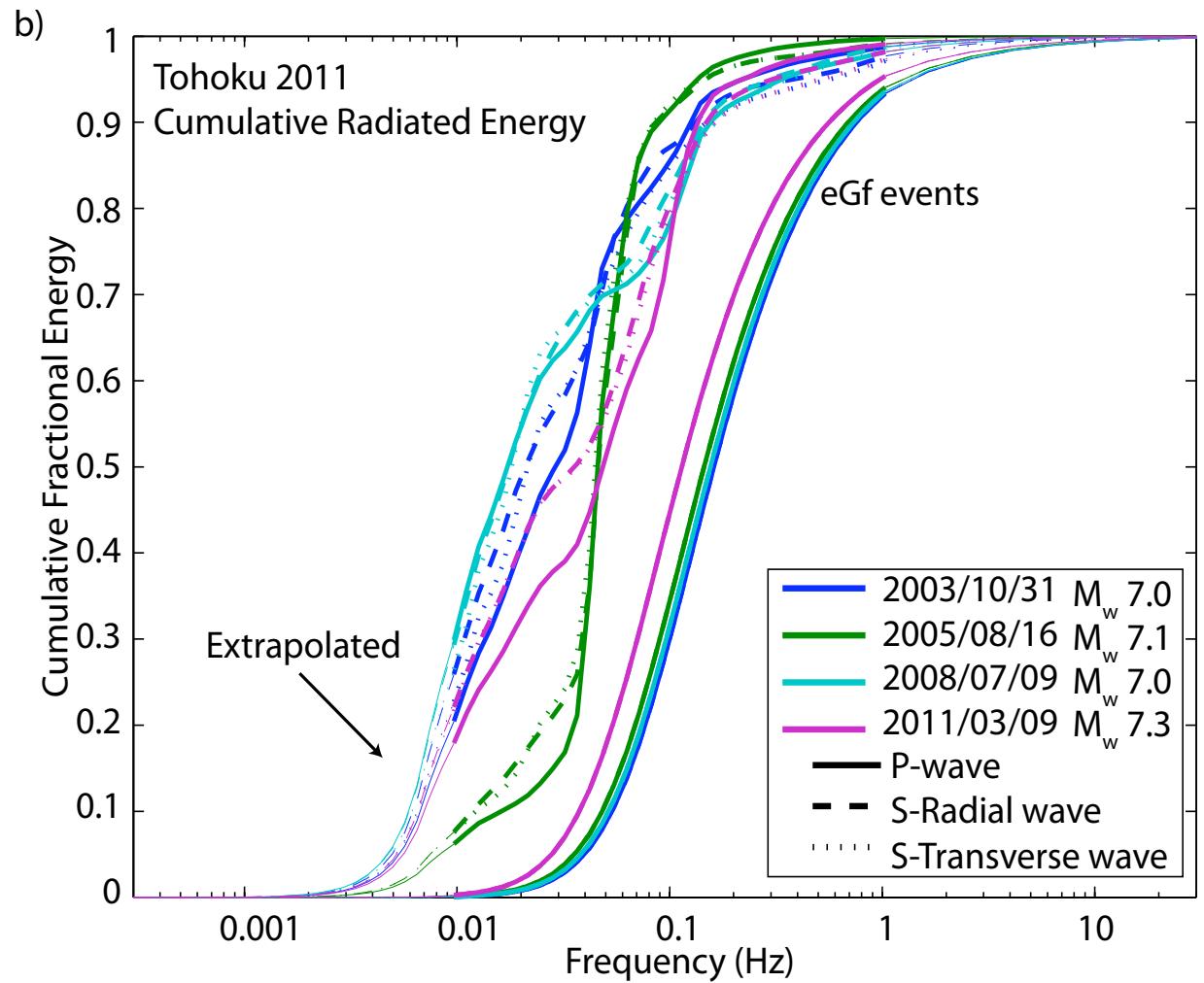


$$E_R \sim \int_0^{\infty} |\omega \cdot \dot{M}(\omega)|^2 d\omega$$

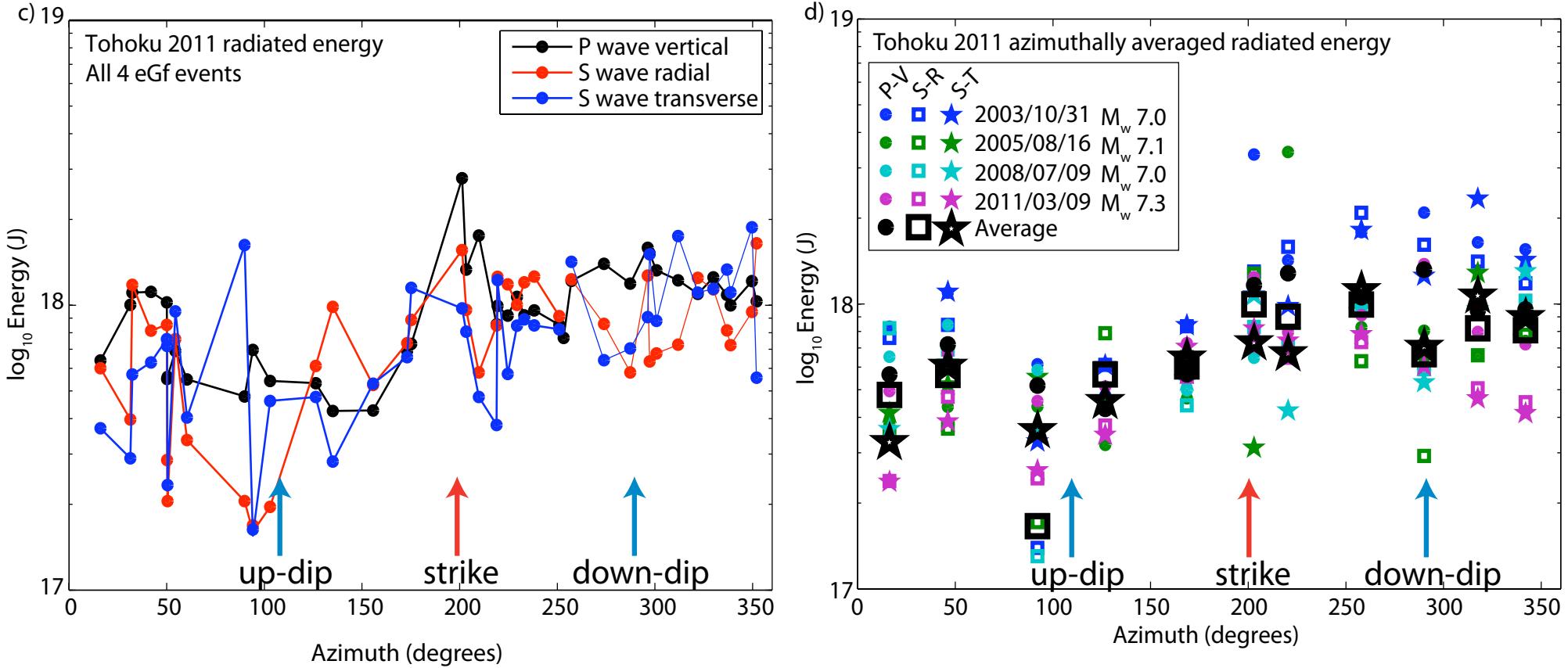
Corner frequency of mainshock is not well resolved
→ Can't measure $\Delta\sigma$

Frequency-Energy Accumulation

- Most energy in 0.01-0.1 Hz band, given very large size/ low corner frequency
- High frequency contribution is negligible (as expected)
- P and S waves are similar for each eGf



Directivity of Seismic Energy



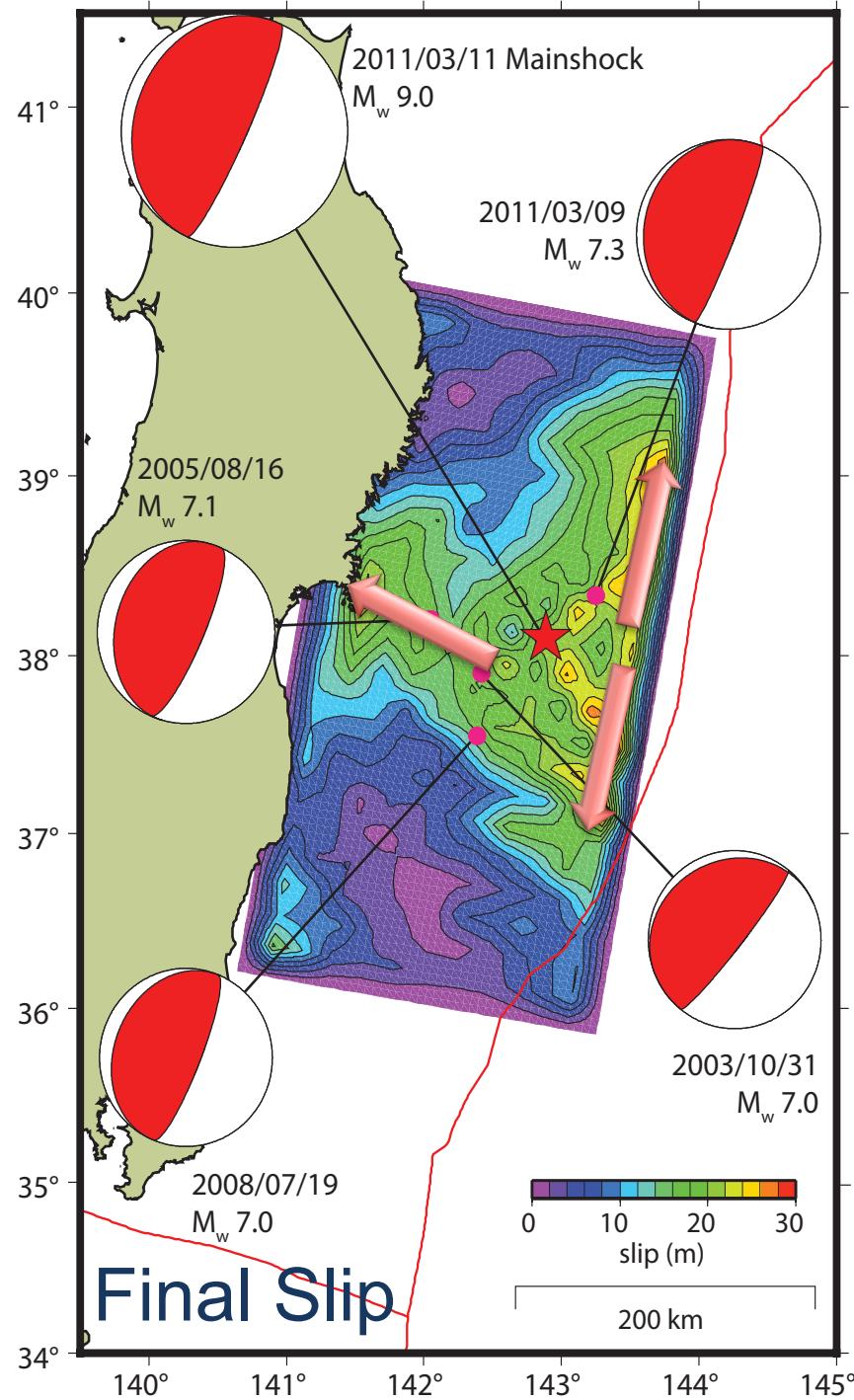
$$E_s = 7.06 \times 10^{17} \text{ J}$$

$$E_s/M_o = 1.57 \times 10^{-5}$$

$$\tau_a = 0.61 \text{ MPa}$$

→ Typically, expect higher energy in direction of rupture propagation

Slip Evolution

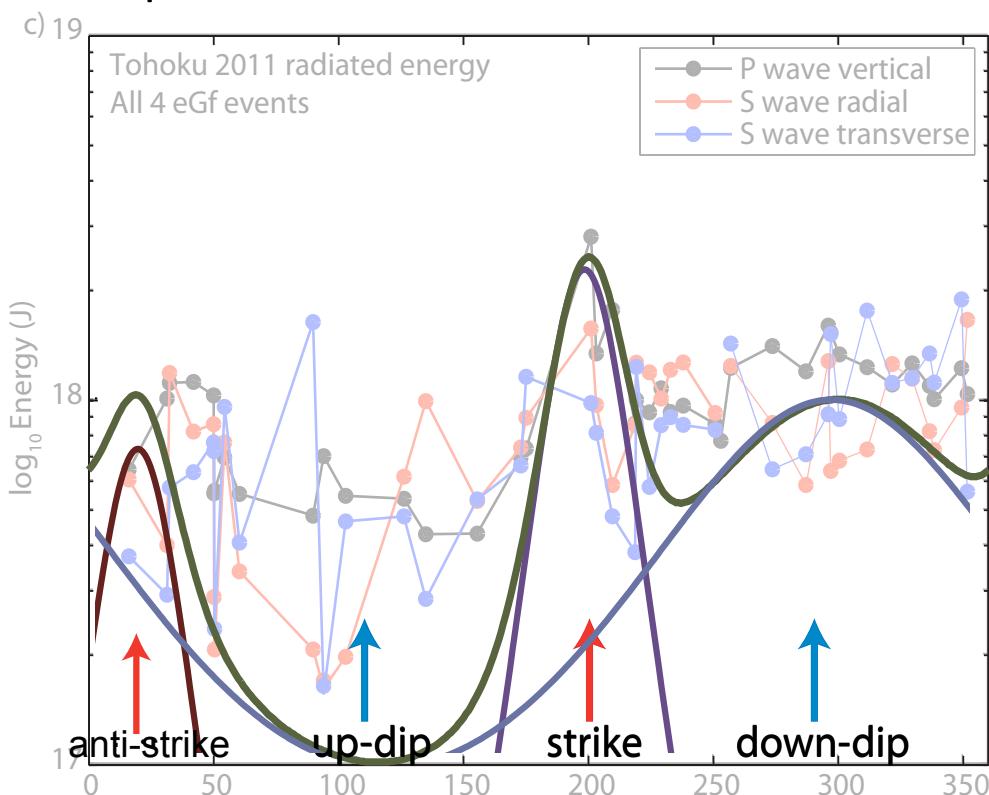


- Slow start
- Down-dip propagation from ~20 s to 40 s
- Rapid, along trench propagation ~50 s to 70 s with large slip

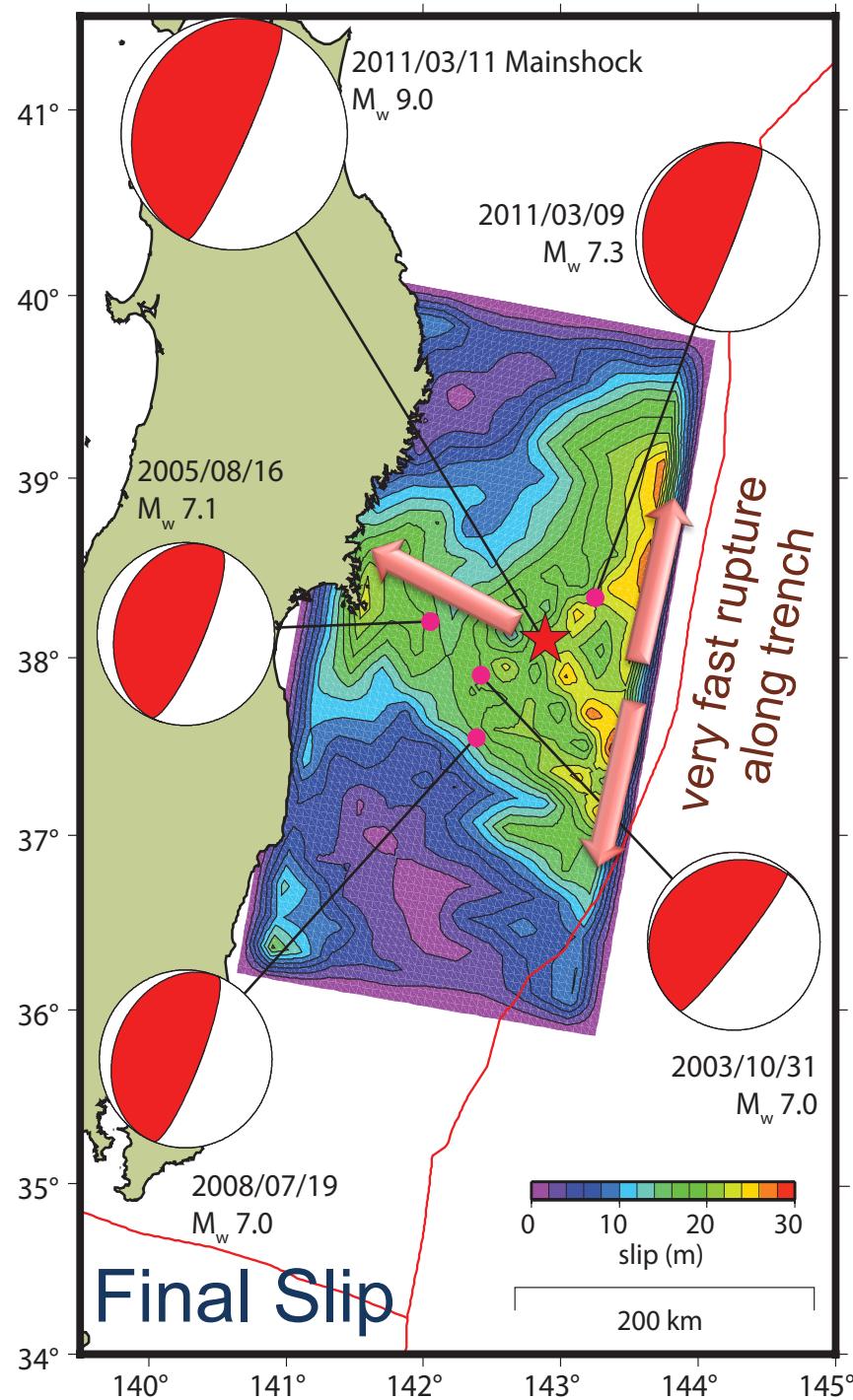
Line Sources

Model simple Haskell line sources

- Rupture direction
- Rupture dimensions
- Rupture velocity
- Amplitude

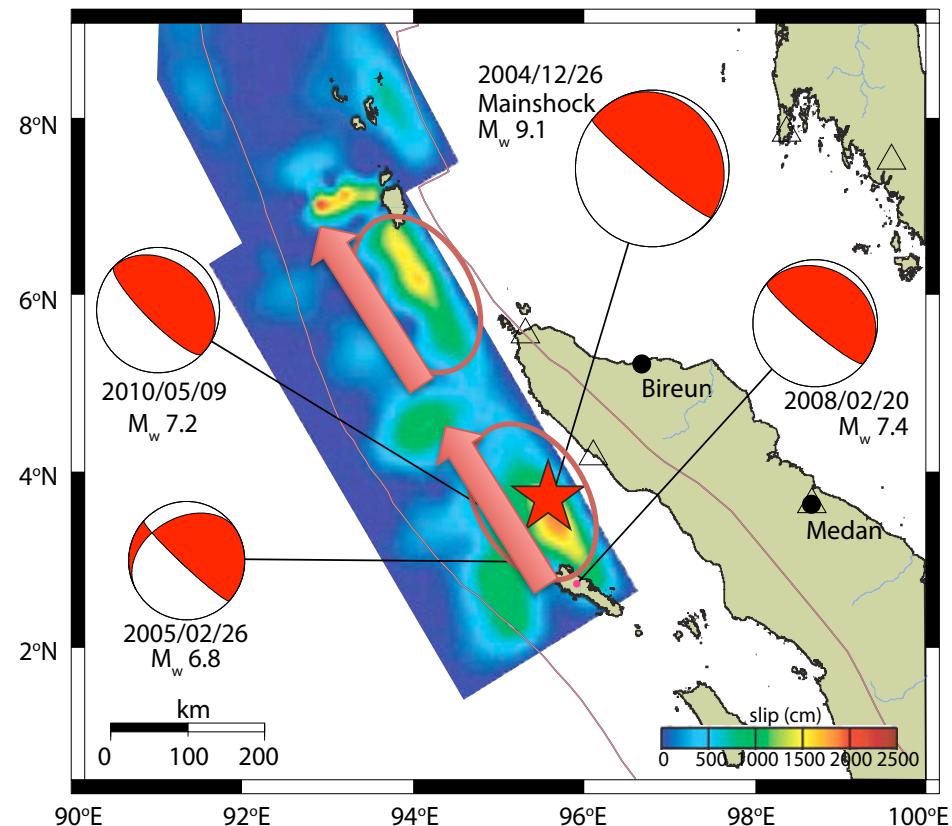
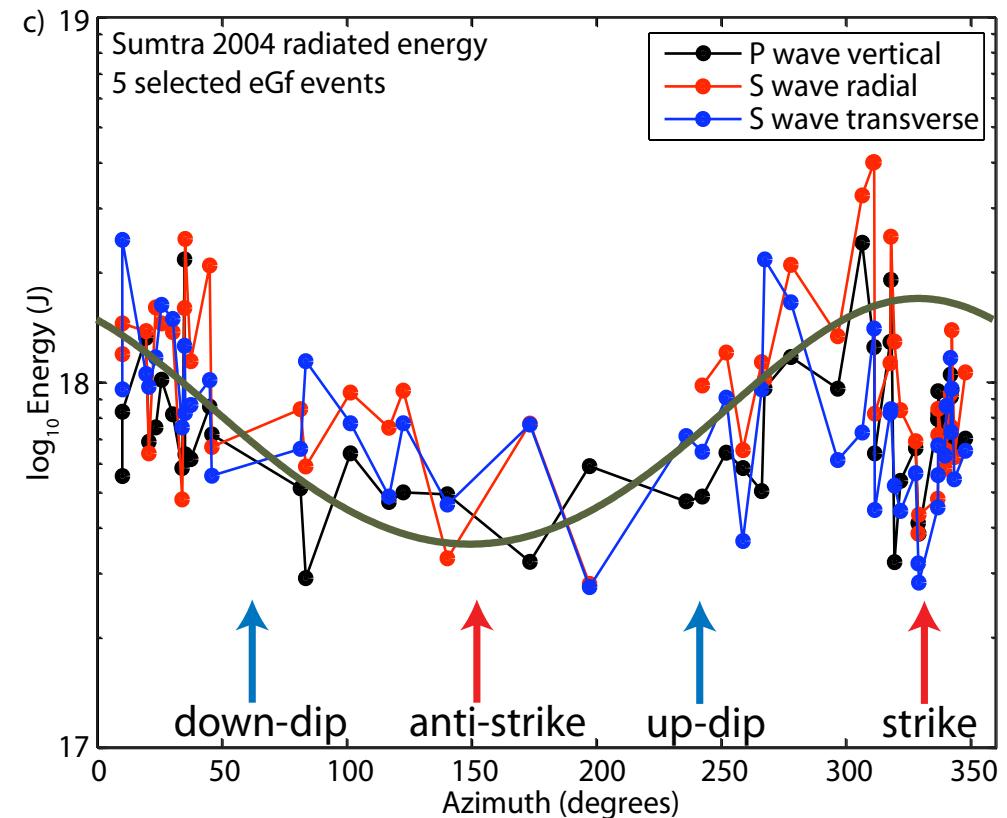


Simple model of rupture captures gross directivity pattern



Sumatra 2004 M_w 9.2

2 Haskell line sources
with half of the moment each



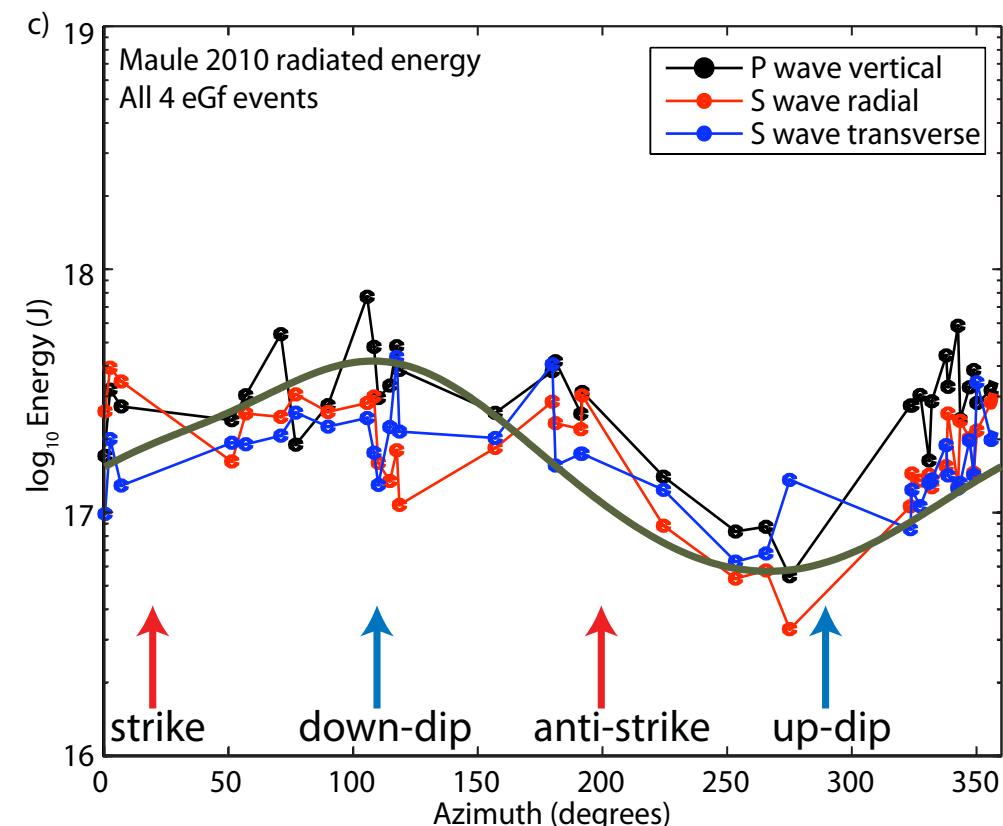
Mean from 3 egf events, 3 components, and 46 stations

$$E_s = 7.25 \times 10^{17} \text{ J} \quad E_s/M_o = 1.1 \times 10^{-5} \quad \tau_a = 0.43 \text{ MPa}$$

Slip inversion from
Ammon et al, [2005]

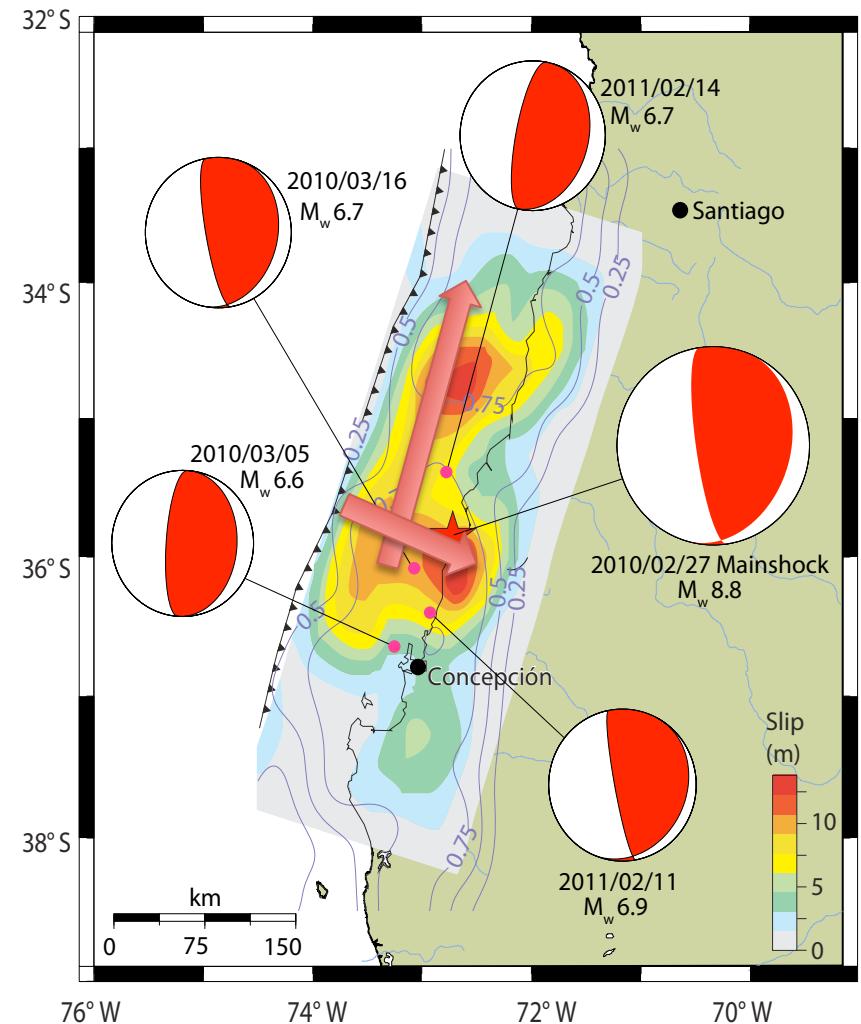
Maule, Chile 2010 M_w 8.8

Source along strike with 50% of moment
Secondary down dip



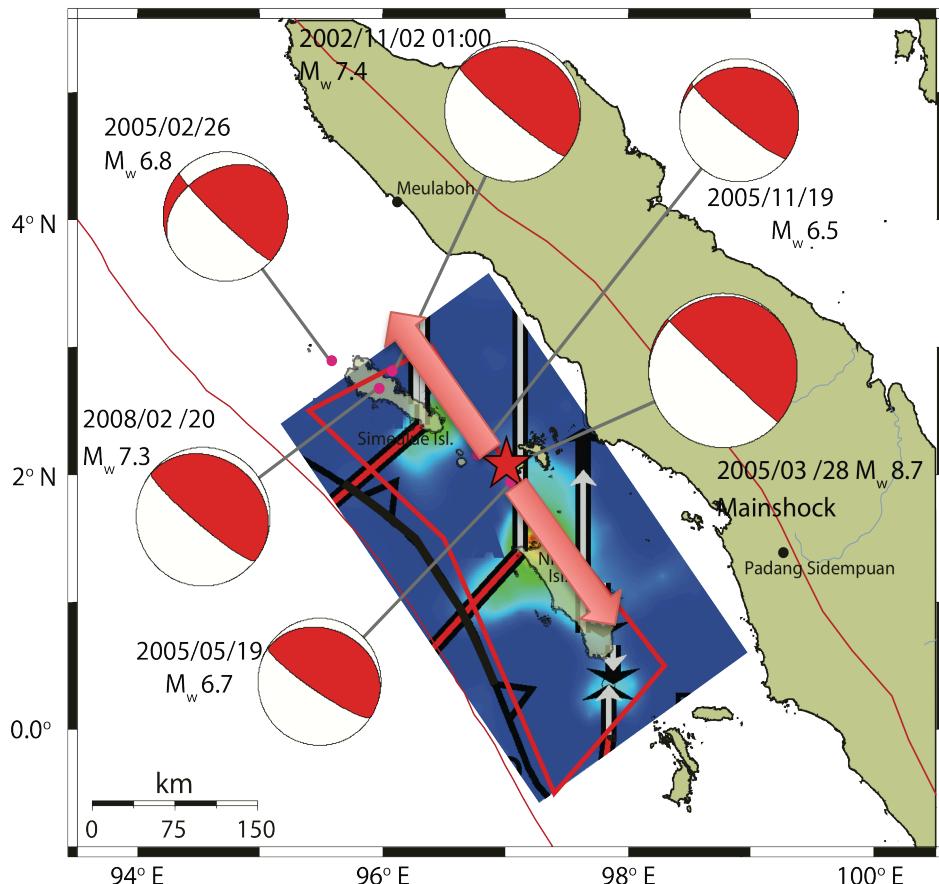
Mean from 4 egf events, 3 components, 35 stations

$$E_s = 1.86 \times 10^{17} \text{ J} \quad E_s/M_0 = 1.0 \times 10^{-5} \quad \tau_a = 0.40 \text{ MPa}$$



Slip inversion from
Hayes 2010

Nias, Sumatra 2005 Mw 8.7

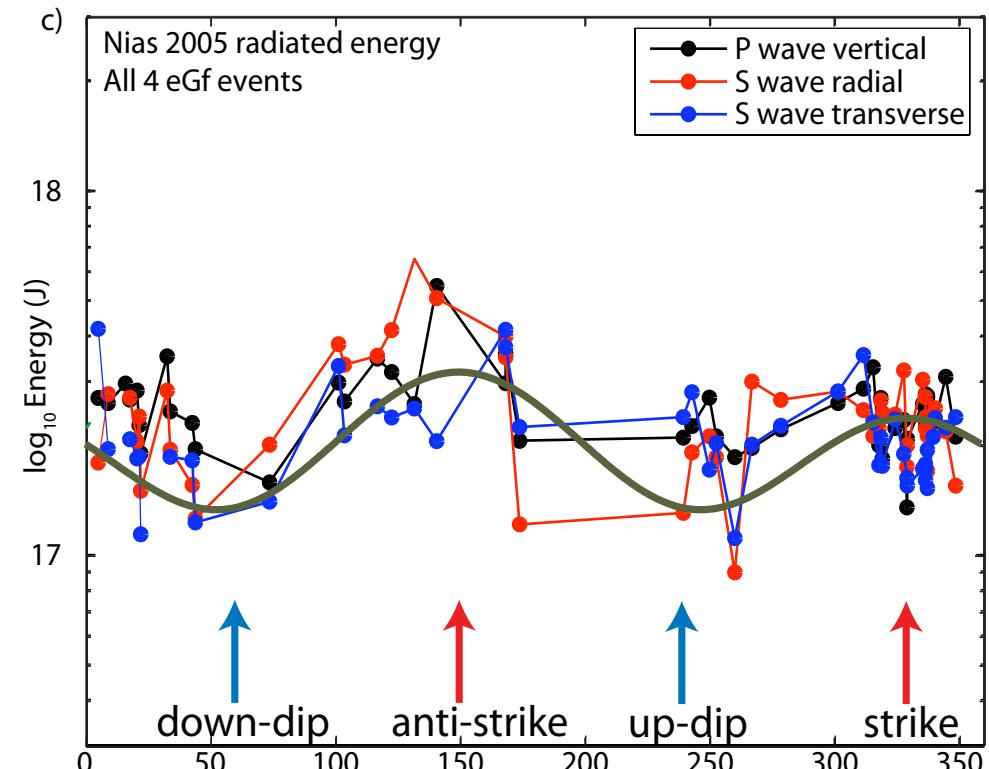


Bilateral rupture

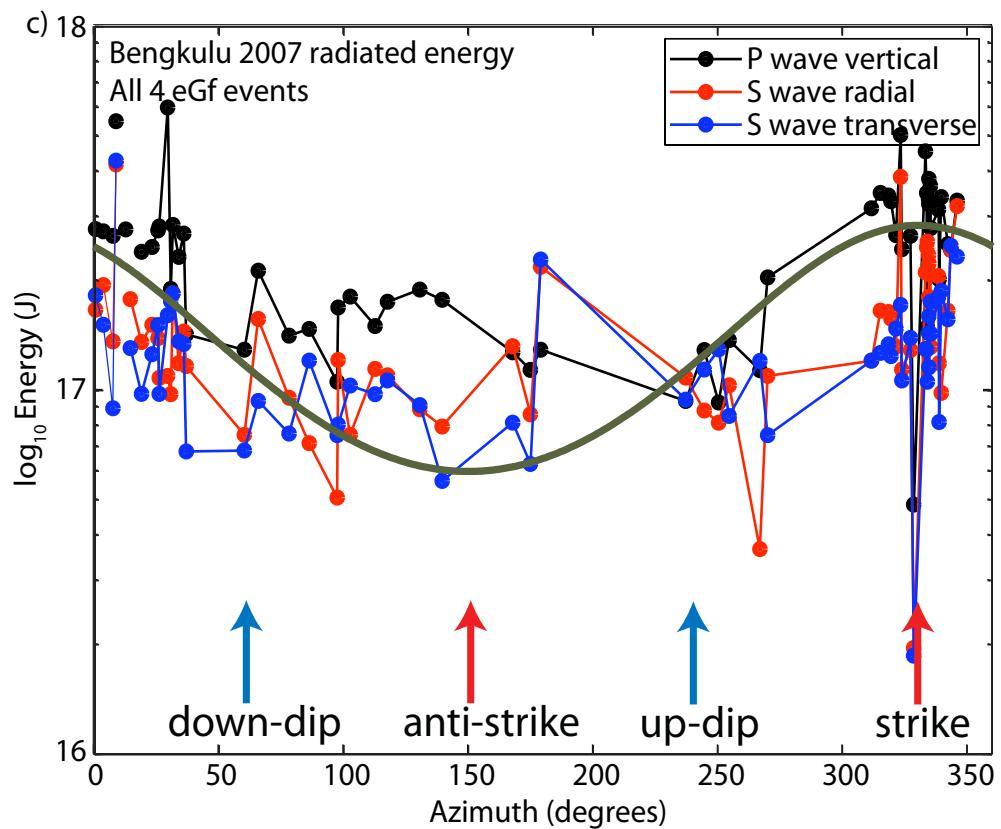
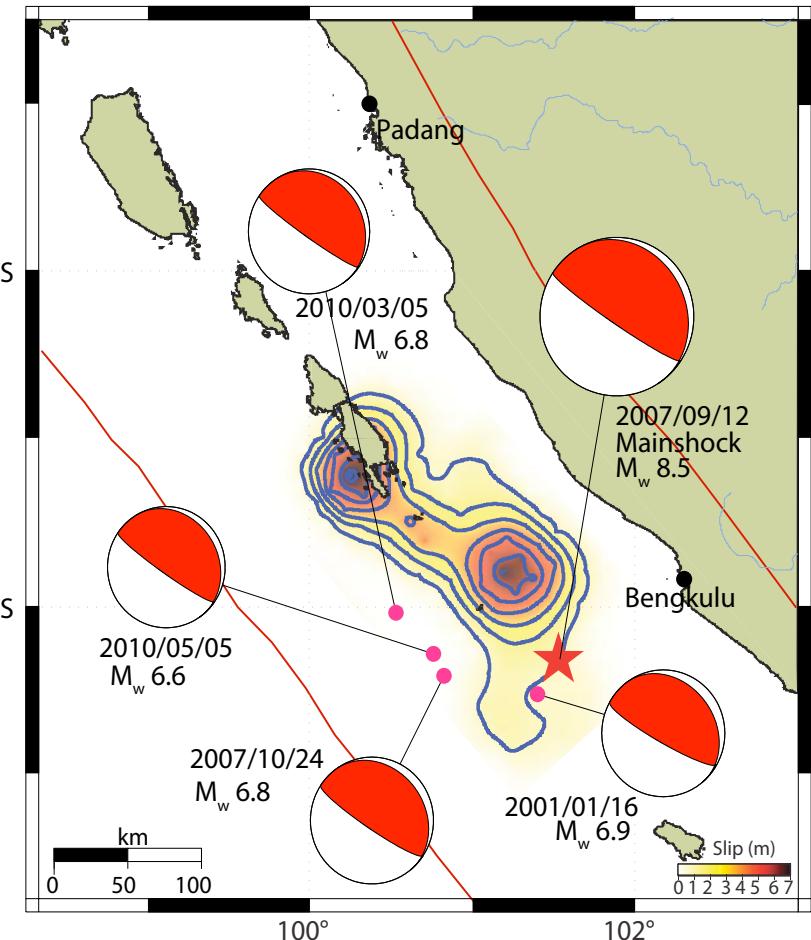
Mean from 4 egf events, 3 components, and 64 stations

$$E_s = 2.19 \times 10^{17} \text{ J} \quad E_s/M_0 = 2.09 \times 10^{-5} \quad \tau_a = 0.81 \text{ MPa}$$

Slip inversion from
Konca et al. [2007]

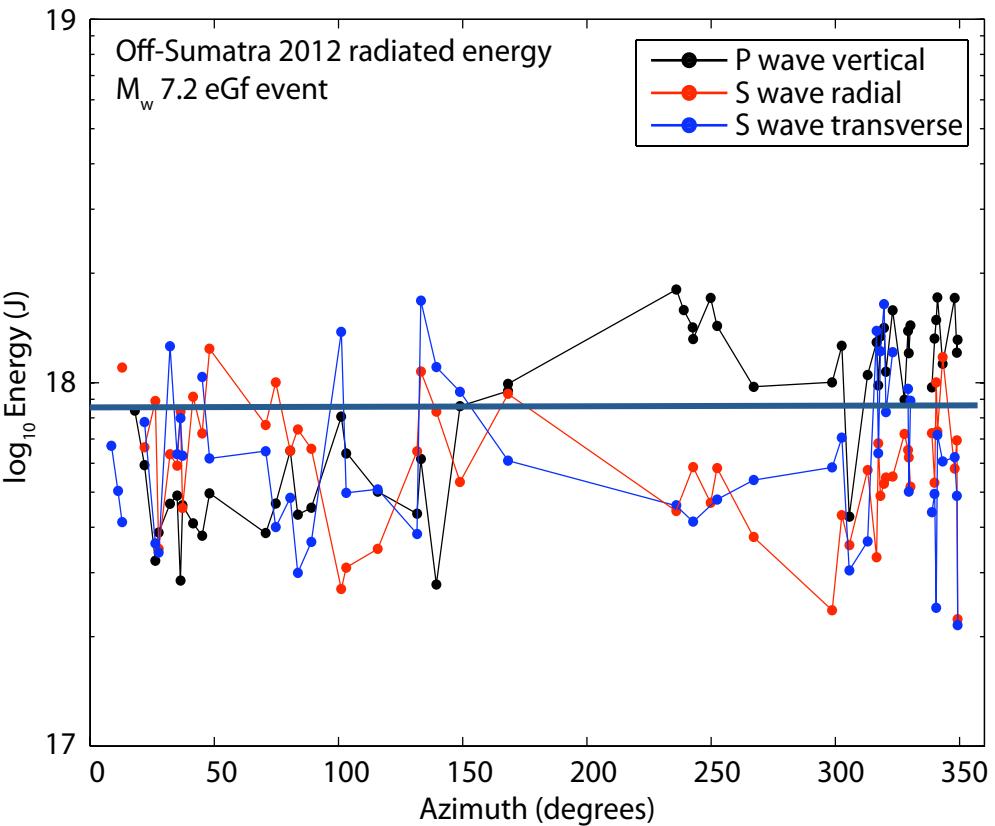
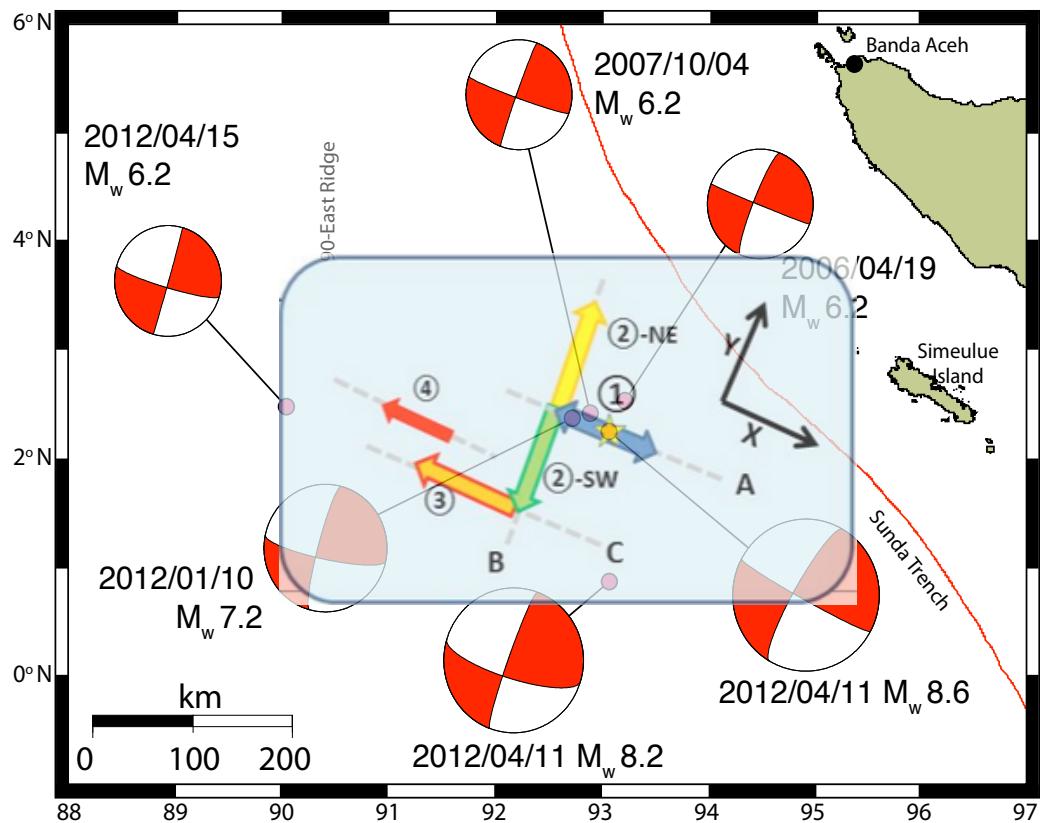


Bengkulu, Sumatra, 2007 Mw 8.5



Mean from 4 egf events, 3 components, 57 stations
 $E_s = 1.33 \times 10^{17} \text{ J}$; $E_s/M_o = 1.98 \times 10^{-5}$ $\tau_a = 0.77 \text{ MPa}$

Off-Sumatra, 2012 Mw 8.6



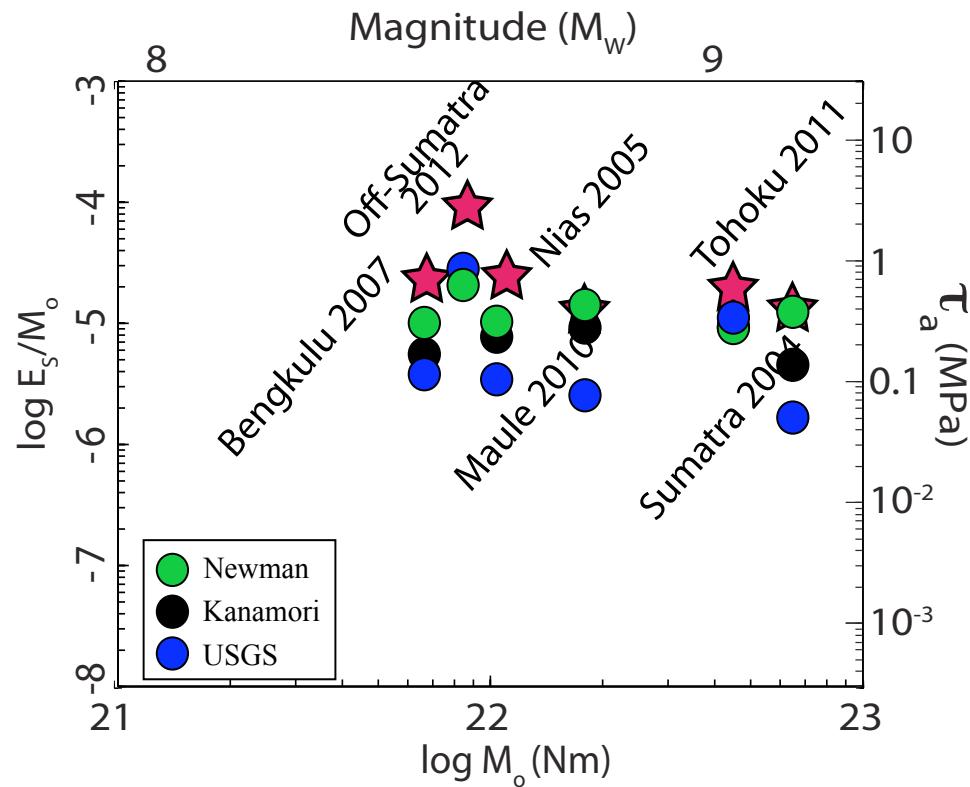
Mean from largest egf, 3 components, 32 stations
 $E_s = 6.71 \times 10^{17} \text{ J}$; $E_s/M_o = 7.89 \times 10^{-5}$ $\tau_a = 3.07 \text{ MPa}$

Greatest apparent stress of all great earthquakes
 - Strike slip - Deep oceanic lithosphere

Slip inversion from

Meng, Ampuero and Luo, 2012

Great Earthquake Apparent Stress

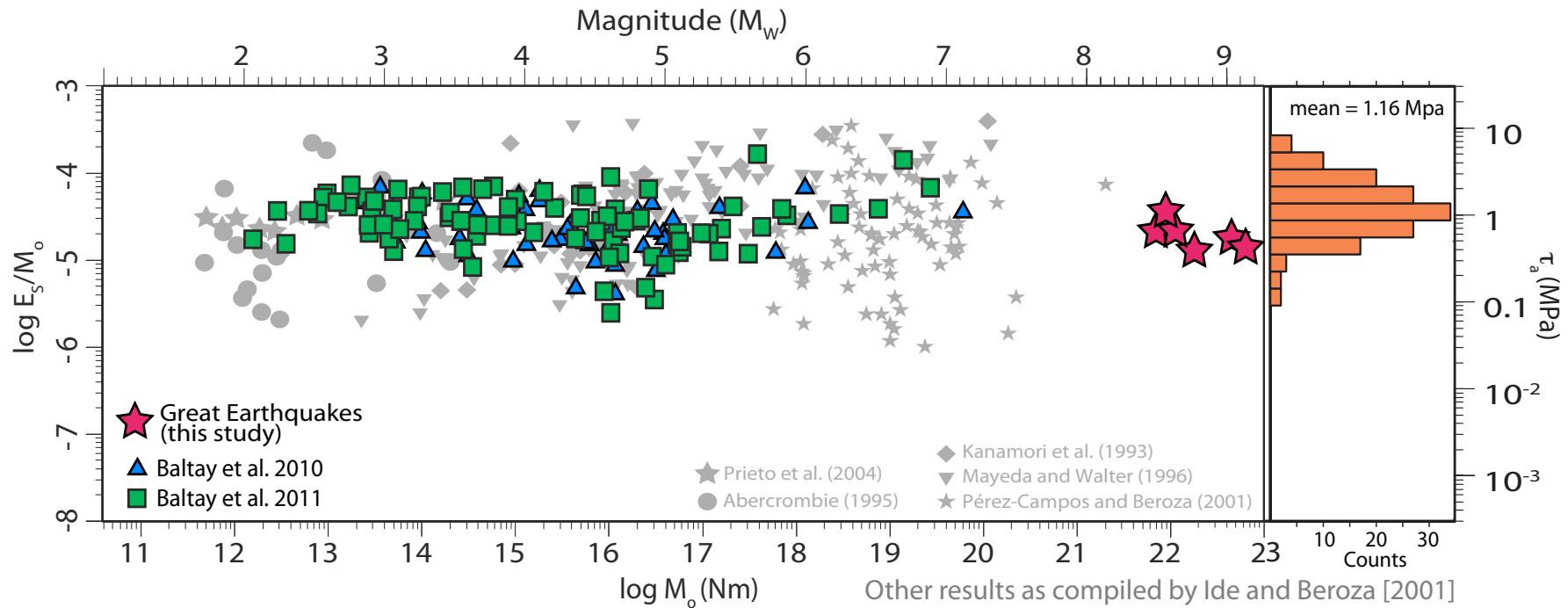


Event	Radiated Energy, E_R (Joules $\times 10^{17}$)				E_R/M_o ($\times 10^{-5}$)	τ_a (MPa)
	Newman	Kanamori	USGS ⁵	This study		
Tohoku-Oki 2011	4.2 ¹	4.3 ³	5.1	7.06	1.57	0.61
Sumatra 2004	8.2 ²	3.0 ⁴	1.1	7.25	1.12	0.43
Maule 2010	2.6 ²	1.7 ³	0.47	1.86	1.03	0.40
Nias 2005	1.1 ²	0.83 ⁴	0.37	2.19	2.09	0.81
Bengkulu 2007	0.69 ²	0.38 ³	0.26	1.33	1.98	0.77
Off-Sumatra 2012	2.1 ¹		2.7	6.71	7.89	3.07

Radiated Energy of Great Earthquakes

- Develop novel teleseismic eGf deconvolution method
- Can correct great earthquakes with $\sim M 7$ eGf events, despite complex rupture
- P and S waves give consistent results, comparable to other studies
- Overall radiated energy is a mixture of both high and low frequency radiation, and we can model some of this dependence through directivity with simple line sources and time dependent source inversions.
- Time dependent eGf source inversions would enlighten the azimuthal directivity further

Compiled Results



- EQs $M \sim 2$ to $M \sim 9$ have constant τ_α and no moment dependence
- τ_α ranges from 0.1 to 10 MPa with mean ~ 1 MPa, log-normal distribution
 $\Delta\sigma$ ranges from ~ 1 to 30 MPa, with mean ~ 6 MPa
- Considerable variability in $\Delta\sigma$ and τ_α is inherent source variability
- Supports self similar earthquake models