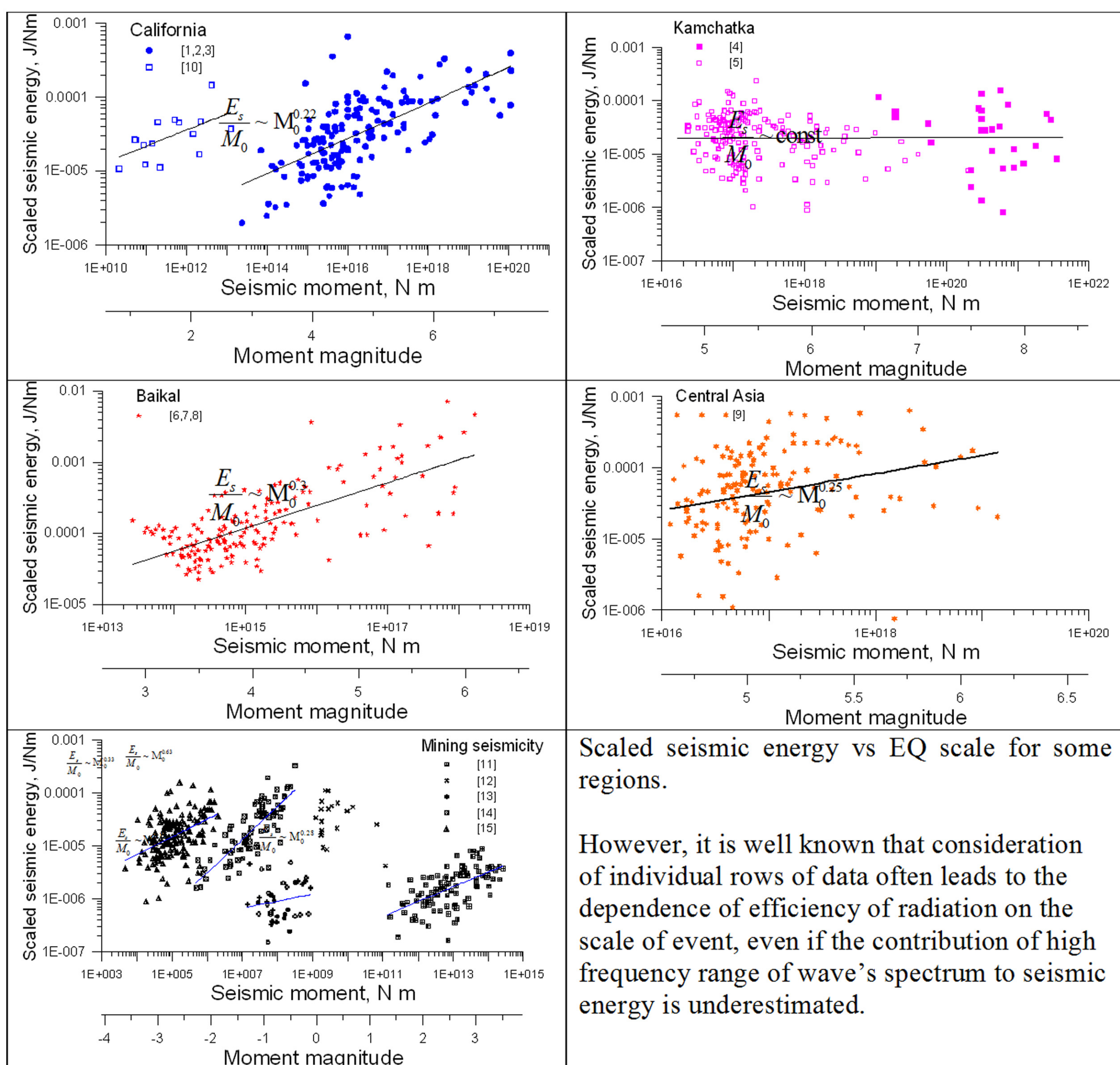


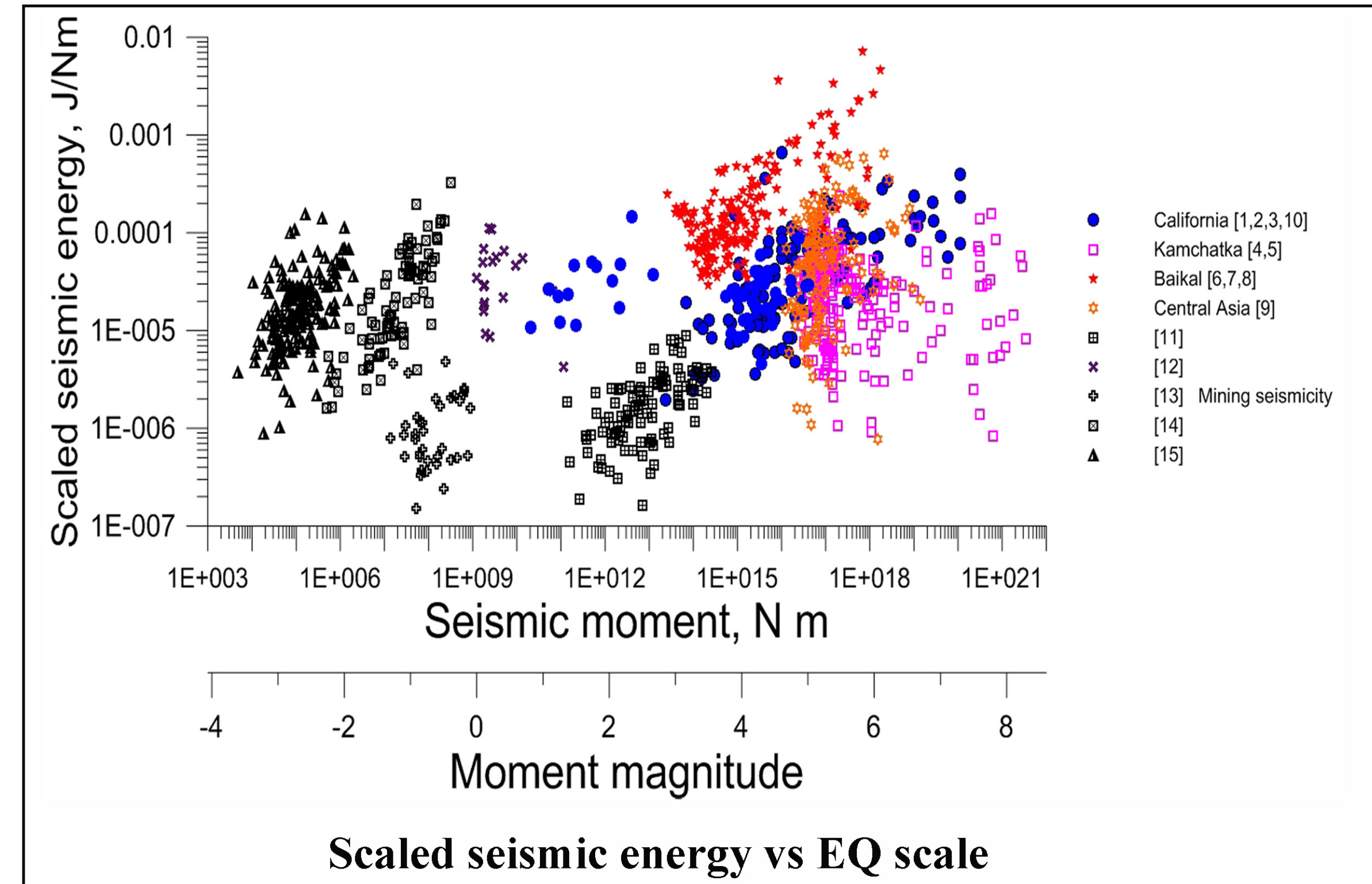
THE FAULT STIFFNESS AS THE KEY PARAMETER THAT CONTROLS EQ EFFICIENCY SCALING LAW

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It is well known that earthquakes have different mechanical efficiencies. Fraction of the energy emitted in the form of seismic waves can vary widely. It is usually assumed that the tectonic earthquake seismic energy E_s is of the order of a few percent of the total potential energy change ΔE_e . However, in some cases this ratio differs significantly. So, tsunami earthquakes have the ratio $E_s/\Delta E_e$ one - two orders of magnitude lower, and for the so-called silent earthquakes E_s becomes negligible. It is clear that the characteristics of radiated seismic waves are defined by the rupture velocity. The slower the rupture, the less energy is radiated in comparison to the scalar seismic moment M_0 .

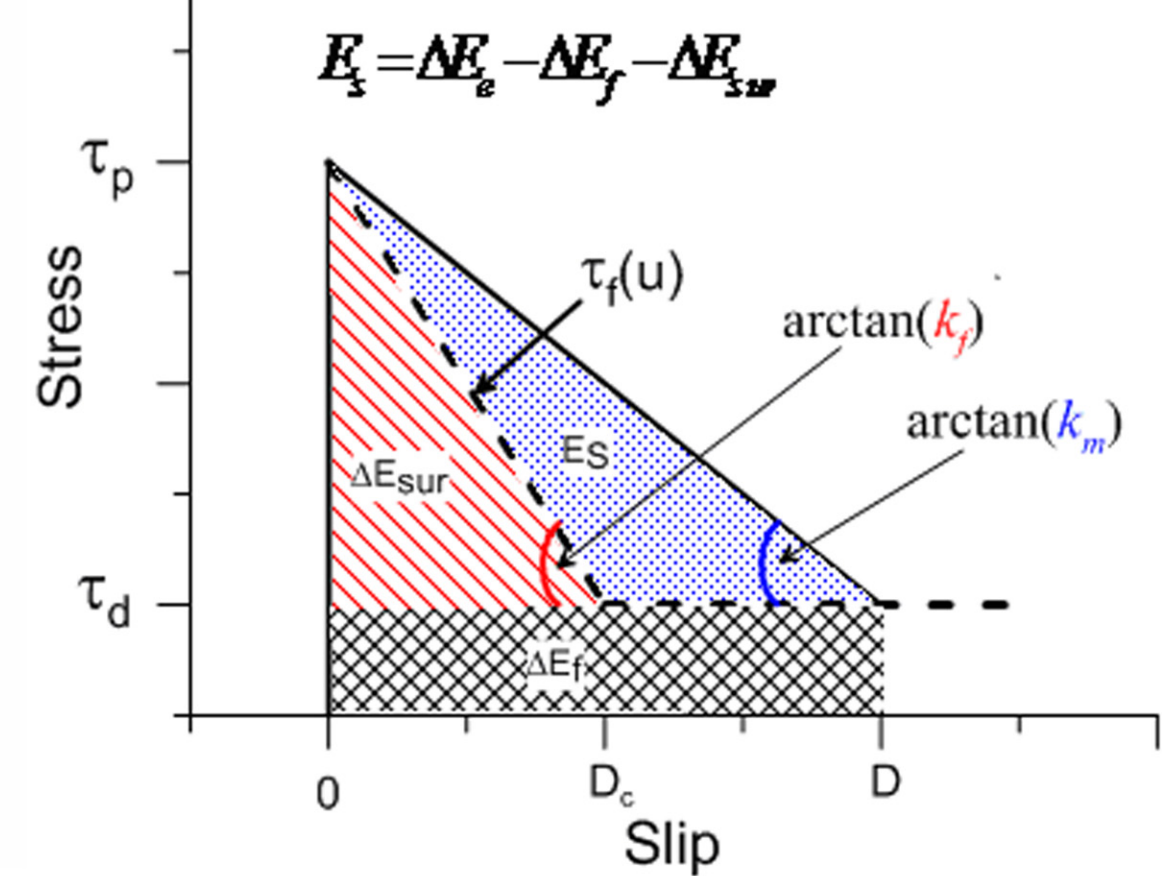


If one changes the seismic moment by 19 orders of magnitude, almost all the data lie in the range $E_s/M_0 \sim 10^{-6}$ - 10^{-3} . Thus, in the full range of data, no dependence of this ratio on earthquake scale is detected, which corresponds to the self-similar medium with linear characteristics.

1 – (Kanamori et al., 1993); 2 – (Mori et al., 2003); 3 – (Mayeda et al., 1996); 4 – (Venkataraman, Kanamori, 2004), 5 – (www.emsd.ru/); 6 – (Dobrynina, 2011); 7 – (www.seis-bykl.ru/); 8 – (Kluchevsky, 2002); 9 – (www.kncd.kz); 10 – (Ide, Beroza, 2001); 11 – (Domański, Gibowicz, 2008); 12 – (Yamada et al, 2007); 13 – (Oye et al. 2005); 14 – (Urbancic, Young, 1993); 15 – (Gibowicz et al., 1991)

- What macroscopic parameters could be markers of the earthquake radiation efficiency?
- Is the specific slip mode at a particular location an inherent property of the fault, or determined by transient conditions?
- Is EQ efficiency the same in all magnitude ranges or there is some scaling law?

Rupture energy budget



Seismic efficiency $\eta = \frac{E_s}{\Delta E_e}$. Radiation efficiency $\eta_R = \frac{E_s}{E_s + \Delta E_{sur}} = \frac{2\mu E_s}{\Delta \tau M_0}$

(Kanamori, Brodsky, 2004). $\eta_R \geq \eta$. If $\eta_R \approx 1$, the breakdown zone is unimportant and friction-dominated failure occurs. If $\eta_R \ll 1$, the microscopic and macroscopic fracturing processes dominate.

Scaled energy $\frac{E_s}{M_0}$ is a convenient parameter to characterize radiation efficiency.

Radiation efficiency

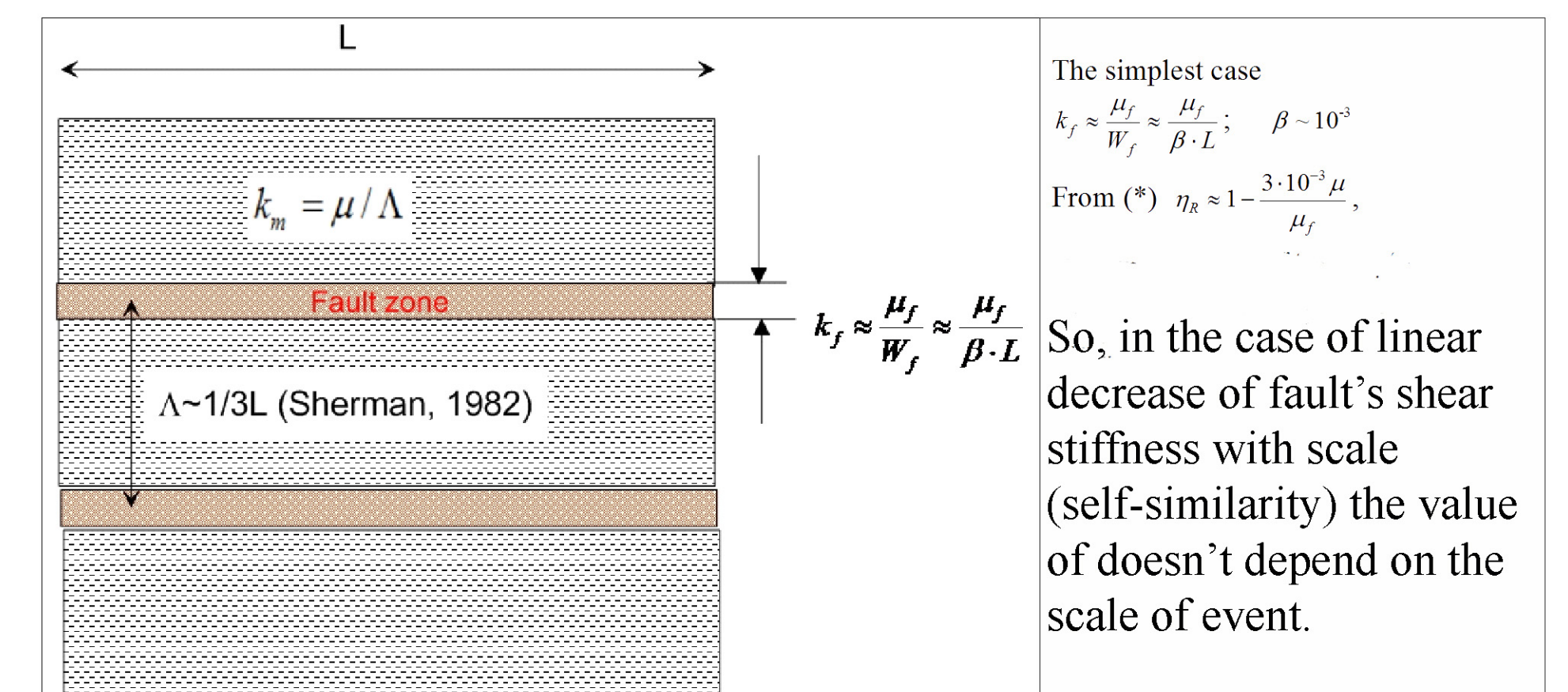
$$\eta_R = \frac{E_s}{E_s + \Delta E_{sur}} = \frac{2\mu E_s}{\Delta \tau M_0} = \frac{D \cdot \Delta \tau - D_c \cdot \Delta \tau}{D \cdot \Delta \tau} = 1 - \frac{D_c}{D} = 1 - \frac{k_m}{k_f}$$

$$\Delta \tau = \tau_p - \tau_d \approx k_m \cdot D \approx k_f \cdot D_c$$

$k_m = \mu/\Lambda$ - stiffness of enclosing massif $\Lambda \approx \frac{1}{3}L$ (Sherman, 1982)

k_f - fault stiffness

$$\eta_R \approx 1 - \frac{3\mu}{L \cdot k_f} \quad (*)$$



STUDY OF REAL DISCONTINUITIES MECHANICAL PROPERTIES IN SITU

The technique of seismic monitoring of rock discontinuities *in situ*

$$k_m \approx \frac{\pi \cdot \rho \cdot C_p}{T \cdot \sqrt{K^2 - 1}}$$

$$k_s \approx \frac{\pi \cdot \rho \cdot C_s}{T \cdot \sqrt{K^2 - 1}}$$

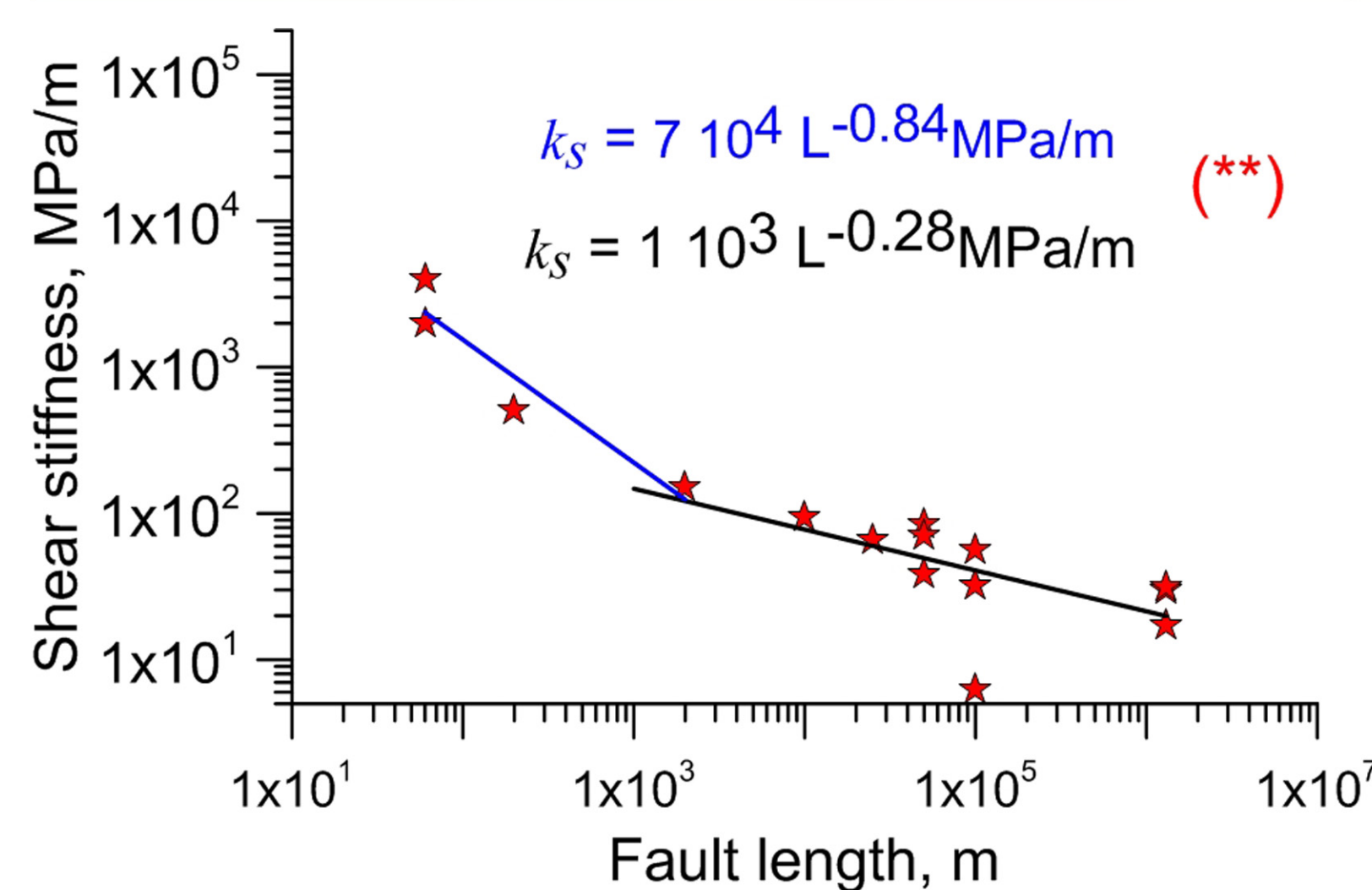
$K = \frac{\text{amplitude of incident wave}}{\text{amplitude of transmitted wave}}$
 T - period of the main phase

$$\sigma(t) = \rho C_p V_{pd}(t) \left(\cos^2 \alpha + \frac{v}{1-v} \sin^2 \alpha \right) + \rho C_s V_{sd}(t) \sin 2\beta$$

$$\tau(t) = \rho C_p V_{pd}(t) \frac{1-2\nu}{2(1-\nu)} \sin 2\alpha - \rho C_s V_{sd}(t) \cos 2\beta$$

$$W_n(t) = \int_0^t [V_x(\tau) - V_x^*(\tau)] d\tau; \quad W_s(t) = \int_0^t [V_y(\tau) - V_y^*(\tau)] d\tau$$

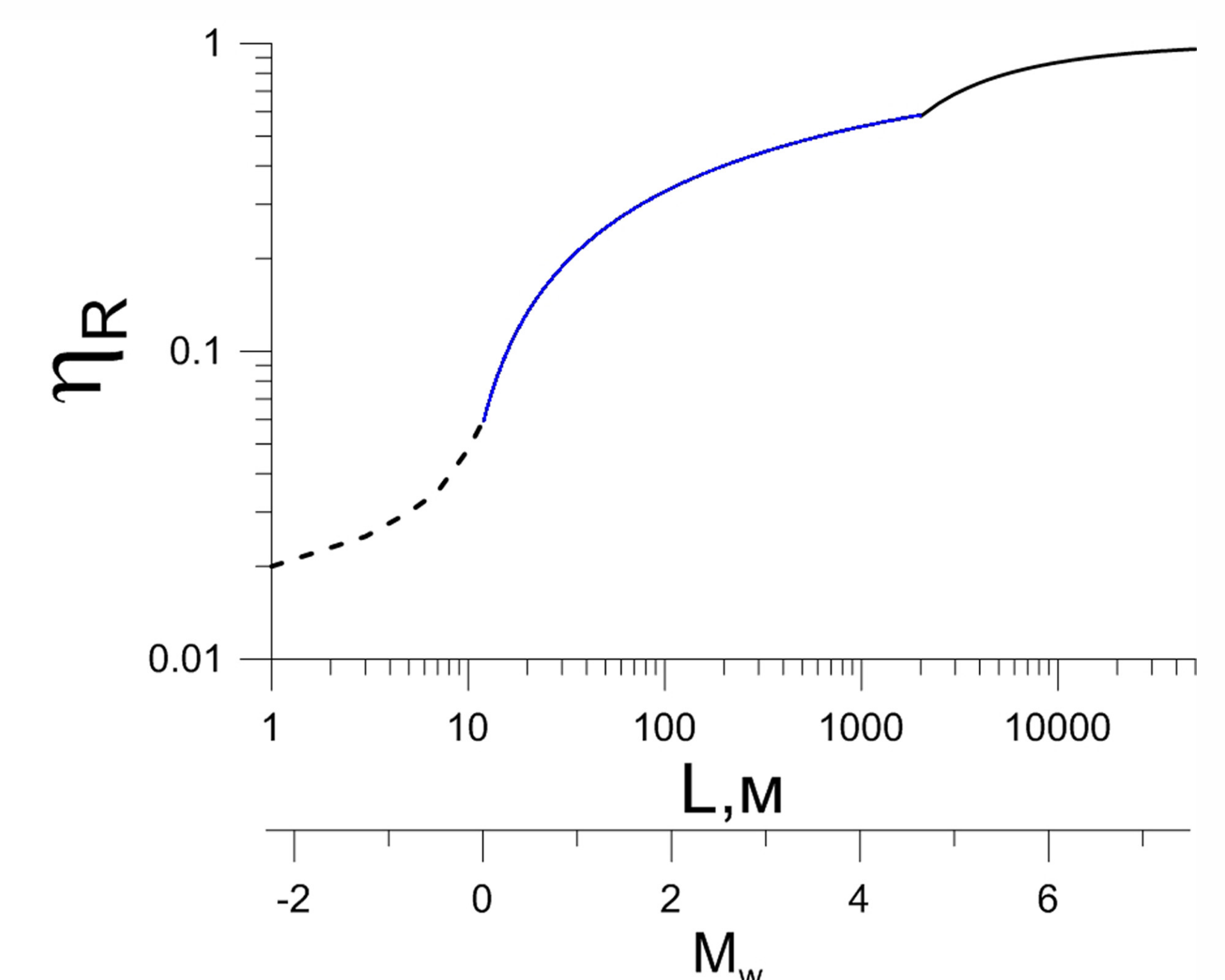
The measurements of the amplitude and time parameters of seismic waves nearby discontinuity give possibility to estimate normal and shear stiffness of the fault or fracture and even to construct stress-strain relation.



ESTIMATIONS OF RADIATION EFFICIENCY

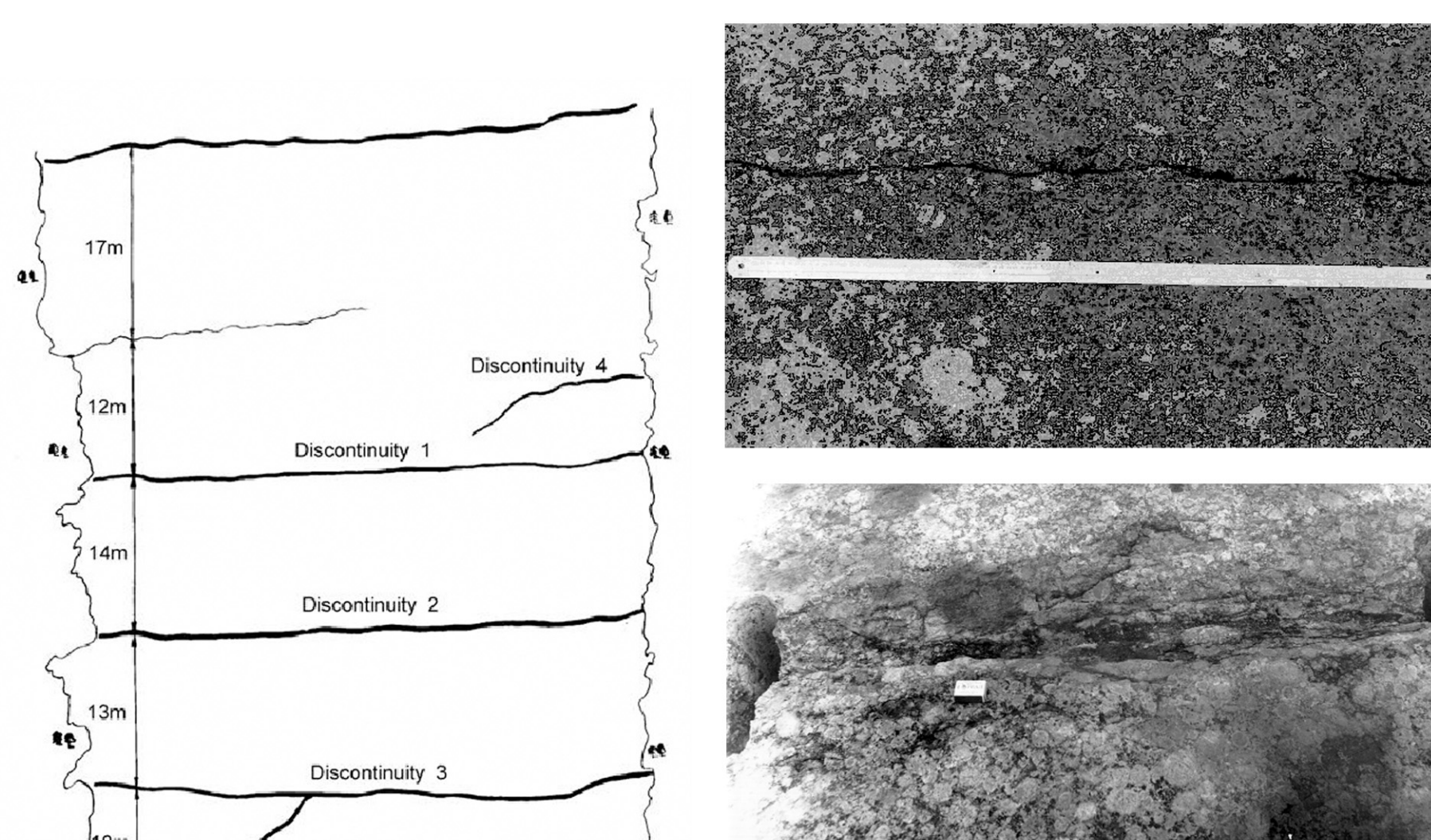
From (*) and (**) radiation efficiency is:

$$\eta_R = \begin{cases} 1 - \frac{1.4}{L^{0.16}}, & 50M < L < 2000M \\ 1 - \frac{100}{L^{0.72}}, & L > 2000M \end{cases}$$



CONCLUSION:

- Fault shear stiffness is the key macroscopic parameter that controls EQ radiation efficiency.
- The value of fault zone stiffness can be estimated *in situ*.
- The mode of sliding (normal EQ, low frequency EQ, very low frequency event, etc. is determined by the current fault zone mechanical properties rather than transient conditions.
- Fault shear stiffness scaling law set the tendency of increasing EQ radiation efficiency with the scale of events.



Small and medium scale
 $Q = 1\text{g}-100\text{kg TNT}$ $L \sim 10^{-4}-10^1\text{m}$

Large Scale $Q = 10^3\text{kg}-10^8\text{kg TNT}$ $L \sim 10^3-10^5\text{m}$

